

Life of Fred
Fractions

Stanley F. Schmidt, Ph.D.



Polka Dot Publishing

A Note to Students

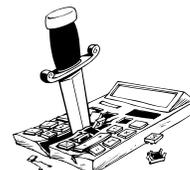
This is the story of one day in Fred's life. He's five years old, but he does some things that many fifty-five-year-olds have never done. Just turn to page 14 when you are ready to start reading about his adventures.

FOR NOW

When you read about what Fred is doing, go as fast as you like, but when you get to the math, please *slow down*. Math is more condensed than English. Most people have to read the math parts more than once in order to fully understand them. If you take your time, it will be enjoyable.

For now, put aside your calculators. Until you get to pre-algebra, one of the most important things you learn is your addition and multiplication facts. Adults who never learned what 7×8 equals are at a disadvantage.

Once you get to pre-algebra, you can take your calculator out of the drawer and use it all you like.



It is not necessary to get rid of your calculator. Just store it somewhere.

YOUR FUTURE

After this book, there are:

- ★ Decimals and Percents
- ★ Pre-Algebra
- ★ Beginning Algebra
- ★ Advanced Algebra
- ★ Geometry
- ★ Trigonometry and
- ★ Calculus

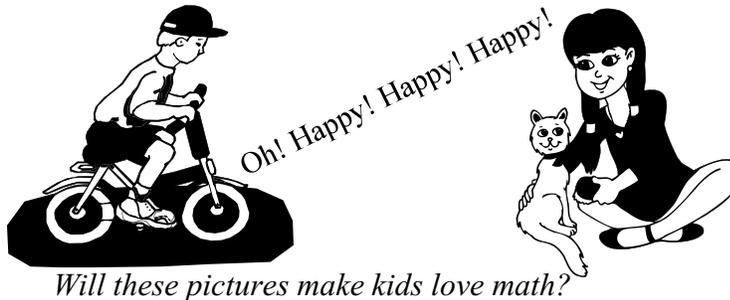
after which, you are ready for university math courses as a junior* and may declare a major in mathematics as soon as your university allows you to.

* A junior at a university is a third-year college student.

A Note to Parents

You know what arithmetic books look like. They are all pretty much alike. Using very few words, they give a couple of examples and then have the students do a hundred identical problems. Then they give another couple of examples and another hundred problems. And for students, arithmetic becomes as much fun as cleaning up their rooms, eating yams, or going to the dentist.

The authors often hope that they can fool their readers by throwing in a couple of irrelevant pictures of happy children at play.



This book, *Life of Fred: Fractions*, takes a slightly* different approach. It tells a story—a story of one day in the life of a five-and-a-half-year-old boy. All of the math arises out of Fred’s life. All of it is motivated—right down to when Fred (in Chapter 23) is working at the PieOne pizza place, and he’s trying to decide whether to put the tomatoes on the pizza before or after it’s cooked, and we get the commutative law.

FACTS ABOUT THE BOOK

Each chapter is a lesson. Thirty-two chapters = 32 lessons.

At the end of each chapter is a *Your Turn to Play*, which gives an opportunity for the student to work with the material just presented. The answers are all supplied. The questions are not all look-alike questions. Some of them require . . . thought!

* “Slightly” in the sense that fish swim slightly better than rocks.

In the Life of Fred series, your daily role in your children's math education is quite minimal. Just make sure that they are writing down the answers to the *Your Turn to Play* questions and encourage them not to cheat by just copying the answers out of the book. You do not need to check their *Your Turn to Play* answers.

As in all of the books in the *Life of Fred* series, the emphasis is on how to learn by reading. *Let the book do the math teaching.* Students of normal academic ability can learn mathematics from Fred without your tutoring the material. You can relax. As students progress through high school, college, and graduate school, they find that less and less is learned in the classroom lecture format. Increasingly, it's the written word that does the teaching. Things changed after Gutenberg.*



*Learning how to learn by reading
is a very valuable skill.*

translation:

Don't short circuit

learning to learn by reading

by your tutoring.

Your more active part in their math education occurs at the end of every four or five chapters. It is called **The Bridge**.



The Bridge consists of ten questions which review everything learned up to that point in the book. Under your supervision, they take out a piece of paper and write the answers to those ten questions. Then, together, you look at the answers that are given in the back of this book.

If they have answered 9 or 10 questions correctly, they have shown that they have *mastery* over the material and have earned the right to go on to the next chapter.

If they don't succeed on the first try, there is a second set of ten questions—a second try—for them to attempt. And a third try. And a fourth try. And a fifth try. Lots of chances to cross the bridge.

* Johannes Gutenberg figured out how to use movable type to print books. In 1455 he printed the Bible.

At the end of the book is **The Final Bridge**, fifteen questions. Again, there are five tries offered.

Life of Fred: Fractions covers a lot more than just how to add, subtract, multiply, and divide fractions. If you'll take a peek at the table of contents, which begins on the next page, you'll see how much is covered. Have you ever wondered why, when you divide fractions,

$$\frac{2}{3} \div \frac{3}{4} \text{ becomes } \frac{2}{3} \times \frac{4}{3} ?$$

Very few arithmetic books tell you *why*—they just say that it's a rule. Fred will give you the reasoning behind the rule.

I guess I should also mention: this book is very silly.

Contents

Chapter 1 Less Than.	14
the symbol $<$	
when to write in a book	
the symbol $>$	
Chapter 2 A Billion.	19
a million	
onomatopoetic words	
minutes to hours to days to years	
Chapter 3 Cardinal and Ordinal Numbers.	23
inches to feet to yards	
writing numbers out in words	
the subjunctive mood	
Chapter 4 Diameter and Radius.	27
Fred's way of teaching	
the meaning of $a < b < c$	
Chapter 5 Fred's Budget.	31
hyperbole	
savings and expenses	
The Bridge (five tries) following Chapter 5.	35
Chapter 6 Doubling.	41
doubling, and doubling, and doubling again	
Chapter 7 Fractions.	44
writing checks	
the meaning of one-half and one-fourth	
sectors	
zero times any number	
the symbol \geq	
the symbol \leq	
Chapter 8 Comparing Fractions.	49
meridian and antemeridian	
multiplying by ten	
Chapter 9 Reducing Fractions.	53
cutting an old comb into six equal pieces	
Chapter 10 Add and Reduce.	56
why you shouldn't run when you are carrying a thirteen-pound knife	
earth to the sun in furlongs	

The Bridge (five tries) following Chapter 10.....	59
Chapter 11 Subtracting Fractions With the Same Denominators.	64
reading marks on a gauge	
general rule: reduce fractions in your answer as much as possible	
general rule: a fraction with zero on top is equal to zero	
general rule: when fractions are equal to one	
Chapter 12 Common Denominators.	68
numerator	
denominator	
Chapter 13 Roman Numerals.	71
numerals vs. numbers	
when IIII is used	
dividing CXLVI by XIV	
Chapter 14 Adding Fractions.	76
a 137-word sentence	
bad eating habits	
alliteration	
Chapter 15 Fractions Mean Divide.....	81
for tapirs, $\frac{1}{2} + \frac{1}{2}$ does not equal one	
whole numbers	
the integers	
the imaginary numbers	
The Bridge (five tries) following Chapter 15.....	85
Chapter 16 Least Common Multiple.....	90
selecting a common denominator	
Chapter 17 Improper Fractions.	93
least common denominator	
improper fractions	
mixed numbers	
Chapter 18 Lines of Symmetry.	96
equilateral triangles	
Chapter 19 Division by Zero.....	99
The Bridge (five tries) following Chapter 19.....	102
Chapter 20 Subtracting Fractions.	107
lb. = pound	
Chapter 21 Circumference.....	111
multiplying fractions	
Chapter 22 Multiplying Mixed Numbers.	113
changing mixed numbers into improper fractions	
Chapter 23 Commutative Law.....	116

Chapter 24 Adding Mixed Numbers.	118
The Bridge (five tries) following Chapter 24.	122
Chapter 25 Canceling.	127
Florence Nightingale	
<i>of</i> often means multiply	
Chapter 26 Opposites.	130
definition of a function	
inverse functions	
Chapter 27 Area of a Rectangle.	134
goal posts: high school vs. college	
Chapter 28 Unit Analysis.	137
rules for kitties	
dimensional analysis	
square of a number	
square roots	
Chapter 29 Subtracting Mixed Numbers.	141
borrowing	
The Bridge (five tries) following Chapter 29.	144
Chapter 30 Division by a Fraction.	149
credit card applications	
how to divide by a fraction	
why you invert and multiply	
Chapter 31 Geometry.	156
Boyle's law of gases	
diagonals of a plane figure	
vertex of a plane figure	
right angles	
parallel lines	
Chapter 32 Estimating Answers.	160
The Final Bridge (five tries) concluding the book.	162
Answers to all the Bridge Problems in the book.	169
Index.	189

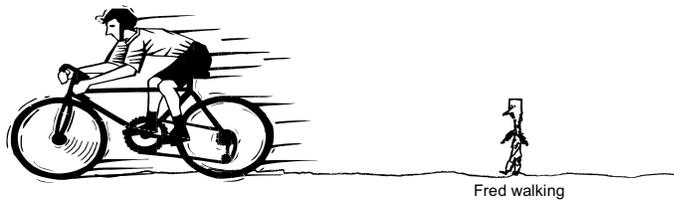
Chapter One

Less Than

When Fred first arrived at KITTENS University he could barely walk. That was because he was only nine months old. A student named Betty became his friend, and she would often carry little Fred so that he could get to class on time.

But that was many years ago. Fred is now $5\frac{1}{2}$ years old. He's no longer a baby who needs to be carried. He walks to class.

Now that he's $5\frac{1}{2}$ years old, he sees things that he never noticed



before. He notices that a lot of students ride bikes. They can go fast. They get to wear helmets, and that looks cool.

Fred thinks to himself, *I want a bike!*

When he was only five years old, he was very happy just walking. But now that he is $5\frac{1}{2}$, he is older.

Fred stopped and took a piece of paper out of his pocket. He started making a list.

	Why I Want a Bike
<input type="radio"/>	
	1. I can get to class faster.
	2. When I'm on a bike, I am taller.
<input type="radio"/>	3. I get to wear a helmet. It would look silly to wear a helmet if I'm just walking.
	4. I will need a lock.
<input type="radio"/>	Locks are fun.

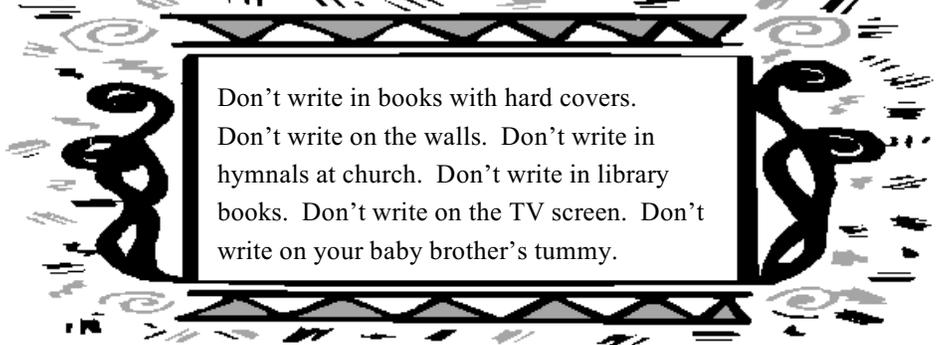
<input type="radio"/>	Why I Want a Bike
	page 2
	5. I am no longer a baby.
	I used to be 5, but
	now I'm $5\frac{1}{2}$.
<input type="radio"/>	$5 < 5\frac{1}{2}$
	6. I can walk at 3 mph.
	On a bike I can go
	10 mph. Everyone
	knows that $3 < 10$.
<input type="radio"/>	Riding is faster.

Before you yell **stop!** again . . .
mph
means
miles per hour

Now it is your turn, my reader, to do some writing. Please get out a piece of paper. When you were a baby, you may have had books that you wrote in. Those workbooks gave you a problem like $2 + 3 = \underline{\quad}$ and you would write in the book: $2 + 3 = \underline{5}$.

You are no longer a baby. If you write in this book, you will mess it up for any younger brothers or sisters who want to read it.

The rule for writing in books—and elsewhere—could be very complicated:



Instead, here is an easy rule:

Write only in books you bought with your own money.

Do you have your piece of paper yet?

At the end of every chapter in this book is *Your Turn to Play*. It is a chance for you to write.

There are three important ways that people learn: reading, hearing, and writing.

Just silently reading the math or just hearing someone read it aloud is not enough.

Your Turn to Play gives you a chance to learn by writing.



Your Turn to Play

1. On your paper, write the three words that finish this sentence:

The symbol $<$ stands for. . .

2. Is $88 < 92$ true or false?

3. Is $100 < 12$ true or false?

4. Is $5 < 5\frac{1}{2}$ true or false? ☺☺☺☺☺ $<$? ☺☺☺☺☺☺☺

5. Fill in any number that makes this true: $14 < \underline{\quad ? \quad}$.

6. Fill in any number that makes this true: $\underline{\quad ? \quad} < 3$.

7. Add $389 + 772$.

8. Make a guess. If $<$ means “is less than,” what does $>$ mean?

..... COMPLETE SOLUTIONS

1. *The symbol $<$ stands for “is less than.”*

2. $88 < 92$ is true.

3. $100 < 12$ is false.

Chapter Twenty-four

Adding Mixed Numbers

Fred hadn't read the instruction book: Prof. Eldwood's *Guide to Making Pizza*, 1851. It gives all the steps:

1. Make crust.
2. Smear with pizza sauce.
3. Add toppings and cheese.
4. Stick in oven.
5. Take out of oven.

Fred had missed the last step. Five chapters ago, he had "popped his 12" Wedding special pizza into the oven." That was a long time ago.

First, it cooked.

Then it dried out.

Then it blackened.

Then it caught on fire.*

Smoke poured out of the oven. The kitchen filled with smoke. Everyone in the restaurant started coughing. Even little lamb in the backyard was affected.

The smoke alarm went off.

The sprinkler system showered everyone.

The fire engines rolled up in front of PieOne.

And Fred was out of a job.



The reporters from the KITTEN Caboodle newspaper arrived. They interviewed Stanthony. They talked with the wet customers. And everyone was pointing at Fred.

The federal disaster-relief group arrived. Six members of Congress were with them. All six got their picture taken with little lamb.

* Did Smoky the Bear ever say, "Things burn better when they're dried out"?

One disaster worker handed Stanthony a package containing a moist little paper towel and told him it was for the lamb. Then the disaster relief group and the members of Congress left.

Fred didn't know what to do. He walked slowly down the street in a daze. The special edition of the newspaper was already published.

THE KITTEN Caboodle



The Official Campus Newspaper of KITTENS UniversityMonday 11:23 a.m. Edition 10*

Disaster strikes! Fred Makes Big Mistake

KANSAS: Disaster struck PieOne at 11:15 this morning. An inattentive trainee named Fred Gauss had left a pizza in the oven for almost an hour. When it caught on fire, smoke and flames were everywhere. The customers all escaped alive, but many had very smoky clothes.



former pizza chef

advertisement

KITTENS Laundry
Special

We'll wash all your
smoky clothes for \$4.

advertisement

PieOne

Two slightly used, smoky
pizzas. Half price.

Your choice:
14" Lamb with Tarragon
8" "Happy Face" Tomato

advertisement

PieOne

Competent Help Wanted

Need a pizza chef who
knows when to take pizzas
out of the oven.

What to do? I don't have any money in my checking account. I'm out of a job, except, of course, for my teaching at KITTENS. But my paycheck for teaching comes at the end of the month.

Fred put his hands in his pockets as he walked down the street. This wasn't the usual way that he walked. He didn't even feel like singing.

Like many five-and-a-half-year-old boys, his pockets were filled with stuff. He could hardly get his hands in his pockets. He stopped at a bench and emptied his pockets onto the bench. Out of his left pocket he pulled $3\frac{3}{4}$ sticks of gum. Out of his right pocket, $2\frac{1}{2}$ sticks of gum.

Well, at least I won't starve, he thought to himself.

Index

<p><..... 15</p> <p>>..... 18</p> <p>≤..... 48</p> <p>≥..... 47</p> <p>alliteration..... 79, 96, 134</p> <p>antemeridian..... 49</p> <p>area of a rectangle..... 135</p> <p>basic rule about car washes..... 137</p> <p>billion..... 20</p> <p>billionths..... 91</p> <p>borrowing..... 142</p> <p>Boyle’s Law..... 156</p> <p>bridges..... 35</p> <p>calculators..... 7</p> <p>canceling..... 128</p> <p>canceling units..... 138</p> <p>cardinal numbers..... 23</p> <p>circumference..... 111</p> <p>common denominator..... 90</p> <p>commutative law..... 116</p> <p>conversion factor..... 139</p> <p>denominator..... 68</p> <p>desert</p> <p style="padding-left: 20px;">the Great Australian..... 62</p> <p style="padding-left: 20px;">the Sahara..... 62</p> <p>diagonals..... 157</p> <p>diameter..... 29</p> <p>dimensional analysis..... 139</p> <p>dividing by fractions</p> <p style="padding-left: 20px;">how..... 151</p> <p style="padding-left: 20px;">why..... 152, 153</p> <p>doubling..... 42, 43, 145</p> <p>ellipse..... 98</p> <p>equilateral triangle..... 98</p> <p>estimating answers..... 161</p> <p>Euripides..... 18</p> <p>Fiddler on the Roof..... 26</p>	<p>Florence Nightingale..... 127</p> <p>football goal posts..... 136</p> <p>function..... 131</p> <p>furlong..... 58, 62</p> <p>general rules..... 66, 67, 101, 112</p> <p>hexagon..... 158</p> <p>hyperbole..... 31, 96</p> <p>imaginary numbers..... 83</p> <p>improper fraction..... 93, 94</p> <p>integers..... 83, 94</p> <p>inverse function..... 132</p> <p>invert..... 152</p> <p>King Solomon..... 83</p> <p>LCM (least common multiple)..... 91</p> <p>least common denominator..... 93</p> <p>least common multiple..... 91</p> <p>libra = lb..... 108</p> <p>line of symmetry..... 97</p> <p>lying vs. laying..... 107</p> <p>man named Giggles..... 100</p> <p>meridian..... 49</p> <p>million..... 52</p> <p>millionths..... 91</p> <p>mirror image..... 97</p> <p>mixed numbers..... 94</p> <p>mixed numbers into improper fractions</p> <p style="padding-left: 20px;">..... 114</p> <p>multiplying fractions..... 111</p> <p>numerals..... 73</p> <p>numerator..... 68</p> <p>oboe..... 123</p> <p>“of” sometimes means multiply..... 129</p> <p>onomatopoetic words..... 20, 62</p> <p>opposite of..... 130, 131</p> <p>ordinal numbers..... 23</p> <p>parallel lines..... 158</p> <p>pentagon..... 158</p>
---	---

Prof. Eldwood's <i>Box Opening the</i> <i>Modern Way</i>	156
Prof. Eldwood's <i>Guide to Modern</i> <i>Medicine</i>	71
quarts into gallons.....	164
radius.	29
reciprocal.	151
reducing fractions.....	54
right angle.....	157
Roman numerals.....	74, 75
sectors.....	47
Shakespeare.	18
Smoky the Bear.	118
square of a number.....	139
square root.	139
subjunctive mood.	26, 60
sum.....	47
tapir.	83
tortoise and the hare.	36
trapezoid.....	104
uncia (Latin) = onza (Italian) = oz.	108
unit analysis.	139
vertex.	157
whole numbers.	83
<i>Wind in the Willows</i>	19, 20
writing in books.	16
zoolatry.....	149

To see what other books
have been written
about Fred
please visit
FredGauss.com