Life of Fred Decimals and Percents

Stanley F. Schmidt, Ph.D.



A Note to Parents

ary Poppins was right: A spoonful of sugar can make life a little more pleasant. It is surprising that so few arithmetic books have figured that out.

Some arithmetic books omit the sugar—which is like lemonade without any sweetener. They give you a couple of examples followed by a zillion identical problems to do. And they call that a lesson. No wonder students aren't eager to read those books.

At the other extreme are the books that are just pure sugar—imagine a glass of lemonade with so much sugar in it that your spoon floats. The pages are filled with color and happy little pictures to show you how wonderful arithmetic is. The book comes with ① a teachers' manual, ② a computer disc, ③ a test booklet, and ④ a box of manipulatives. And they are so busy entertaining the reader that they don't teach a lot of math. This second approach is also usually quite expensive.

We'll take the Goldilocks approach: not too sour and not too sweet. We will also include a lot of mathematics. (Check out the Contents on page 10.) How many arithmetic books include both forms of the Goldbach Conjecture? (See Chapter 17.) The reader will be ready for pre-algebra after completing this book.

This book covers one afternoon and evening of Fred's life and continues the story from *Life of Fred: Fractions*. Every piece of math first happens in his life, and then we do the math. It is all motivated by real life. When is the last time you saw prime numbers actually *used* in everyday life? They are needed in this book when the cavalry is getting ready to attack what the newspaper calls the "Death Monster."

FACTS ABOUT THE BOOK

Each chapter is a lesson. Thirty-three chapters = 33 lessons.

At the end of each chapter is a *Your Turn to Play*, which gives the student an opportunity to work with the material just presented. The answers are all supplied. The questions are not all look-alike questions.

Some of them require . . . thought! Each Your Turn to Play often incorporates some review material. The students will get plenty of opportunity to keep using the material they have learned.

At the end of every five chapters is **The Bridge**, ten questions reviewing everything learned up to that point. If students want to get on to the next chapter, they need to show *mastery* of what has been covered so far. They need to get nine or more questions correct* in order to move on to the new material. If they don't succeed on the first try, there is a second set of ten questions—a second try. And a third try. And a fourth try. And a fifth try. Lots of chances to cross the bridge.

Don't let your students move on without showing mastery of the previous math.

At the end of the book is **The Final Bridge**, consisting of twenty questions. Again, five tries are offered.

RULES OF THE GAME

For now, students should put aside their calculators. This is the last chance we have to cement in place their addition and multiplication facts (which they should have had memorized before they began *Life of Fred: Fractions*.) I balance my checkbook each month without a calculator just to keep in practice.

Once the students get to pre-algebra they can take their calculators out of their drawers and use them all they like.

When the students are working on the *Your Turn to Play* or **The Bridge** sections, *they should write out their answers*. When they are working on a **Bridge**, they should complete the whole quiz first.

banned for now

Then you and your child can check the answers together. This will give you a chance to monitor their progress. Mastery of the material is much more important than speed.

[★] The answers to all of the Bridge questions are given right before the index in the back of this book.

FINAL THOUGHTS

These *Life of Fred* books are designed to teach the material. They are not merely repositories of examples and homework problems. It is so important that kids

learn how to learn from reading.

Once they finish college, they will face forty years in which virtually all of their real learning* will come from *what they read*. It is not a favor to the students for you to repeat what the book said. If you do that, it is a disincentive for them to learn to benefit from their reading.

As strange as it sounds, *you don't need to teach the material*. I've done that work for you. Relax. You can best teach by example. You read your books, while they read theirs.

The best way for you to help is to check their progress when they work on **The Bridges**.

[★] If "real learning" for adults is exemplified by what they see on television—on quiz shows or the educational channels—then the thousands of dollars and the thousands of hours they spent going to college were an utter waste.

Contents

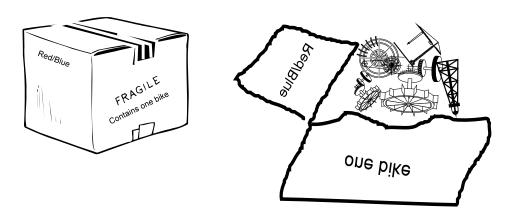
Chapter 1	Number Systems
	decimal numbers
	base 10 system
	vigesimal (base 20) system
	1° = 60 minutes
Chapter 2	Adding Decimals
	grams
Chapter 3	Subtracting Decimals
Chapter 4	Multiplying by Ten
	centimeters
Chapter 5	Pi
	diameter and circumference
	approximately equal to (\approx)
	rounding numbers
The Bri	dge (five tries)
Chapter 6	Multiplying Decimals
	whole numbers
Chapter 7	Functions
	inverse functions
	radius
Chapter 8	Subtracting Mixed Units
Chapter 9	Sets
	elements of a set
	braces
	subsets
	empty set
	set-builder notation
	union, intersection, and difference
Chapter 10	Rules of Divisibility. 53
	when numbers are evenly divisible by 5, 2, and 3
The Bri	dge (five tries)
Chapter 11	Dividing a Decimal by a Whole Number
	when numbers are evenly divisible by 9
	natural numbers
	conversion factors

Chapter 12	When Division Doesn't Come Out Even
	divisor, quotient, and dividend
	changing fractions into decimals
	changing decimals into fractions
Chapter 13	When Division Never Comes Out Even
	using remainders to terminate the division
	using fractions to terminate the division
	repeating decimals and terminating decimals
Chapter 14	Dividing by a Decimal
	when to add, when to subtract, when to multiply, and when to divide
	the reason why $0.0112 \) \ 16.0000$ is the same as 112. $) \ 160000$.
	squaring a number
	billion, trillion, quadrillion, quintillion
	exponents
Chapter 15	Bar Graphs
	vertical bar graphs
	when to use horizontal bar graphs
The Brid	1ge (five tries)
Chapter 16	Prime Numbers
	composite numbers
	consecutive numbers
Chapter 17	Goldbach Conjecture
	his first conjecture
	his second conjecture
	open questions in mathematics
Chapter 18	Area of a Circle
Chapter 19	Dollars vs. Cents
	.50¢ vs. 50¢
Chapter 20	Pie Charts
	what percent means
	circle graphs
	changing fractions into percents
	changing percents into fractions
	changing decimals into percents
The Bri	1ge (five tries)
Chapter 21	40% of 15
	of often means multiply
	theorems and corollaries

Chapter 22	30% off
	why we do mathematics (a small essay)
	double and triple discounts
Chantar 22	Distance = Rate × Time
•	
Chapter 24	15% More
	the hard way to do 15% more
G1 . 25	the easy way to do 15% more
Chapter 25	Area of a Triangle
	mental arithmetic
	Heron's formula
	square root
	altitude of a triangle
	1ge (five tries)
Chapter 26	Area of a Parallelogram
	congruent triangles
Chapter 27	13 Is What Percent of 52
Chapter 28	Ratio
Chapter 29	Ordered Pairs
	mapping and images (functions)
	a third definition of functions
Chapter 30	Graphing
	x-coordinate and y-coordinate
	negative numbers
	how to tell if a graph is the graph of a function
	x-axis and y-axis
The Brid	1ge (five tries)
Chapter 31	Nine Conversions
-	when long division was invented
Chapter 32	Elapsed Time
•	how long to floss your teeth
Chapter 33	Probability
1	events with a probability of 0%
The Fin	al Bridge (five tries)
Answers to	all the Bridge Problems
Index	

Chapter One Number Systems

hat do five-and-a-half-year-old boys dream about? Many things. For Fred it was a new bicycle. When the box arrived at his office, he tore off the tape. The box fell open. Inside was . . . junk. There were gears, wires, rods, and motors, but no bicycle. He had spent every penny in his checking account (\$1,935.06) and didn't get a bike.



Fred had been cheated.

After a short trip with a blanket to a corner of his office to do a little crying, he returned to look at the pile of parts on the floor. There were bags of electrical plugs.

There were springs.

There were springs.

all this stuff? Maybe

I should just throw it all in the garbage.

Then he almost stepped on a huge remote control. It had about 168 buttons on it. And then it came to him: I know! I will build a robot!

Maybe my \$1,935.06 won't be wasted after all.

Let's look at \$1,935.06 for a moment.



1,935.06

This is a decimal number. That's because it contains a decimal point (the dot between the 5 and the 0).

When you studied the whole numbers, $\{0, 1, 2, 3, 4, \dots\}$, you didn't need any decimal points. When you count the number of buttons on a remote control, you get 168, not $168 \frac{3}{4}$ or 168.75 or -5.

When you cut up a pie into sectors, fractions come in handy. At

the dinner table you might ask, "Mom, after you cut Dad's piece—which is one-quarter of the pie

—could I please have the rest?"

Your mother, being good in mathematics, does the computation: $1 - \frac{1}{4} = \frac{3}{4}$ and hands you threequarters of the pie.

But there are times when decimals are more useful than fractions. For example, the bike cost Fred \$1,935.06. You could write that as

\$1935 $\frac{6}{100}$ but that looks a lot messier.

Can you imagine what a car odometer* would look like if instead of displaying: 40528.0

40528.1

40528.2

40528.3

it displayed fractions like:

 $40528 \frac{1}{8} \\ 40528 \frac{1}{4}$

[★] An odometer is the gauge that tells you how far you have gone.

In our number system the position of the digits makes a difference. Would you rather have \$18 or \$81? Both have the numerals I and δ , but where the I and δ sit makes a big difference.*

We use the **base ten** system. When we look at a number like

1,935.06

the digit to the left of the decimal (the 5 in this case) is 5 ones. As we move to the left, each digit is "worth" ten times as much. As we move to the right, each digit is "worth" one-tenth as much.

1,935.06 = 1 thousand

+ 9 hundred

+3 tens

+5 ones

+0 tenths

+ 6 hundredths.

We could say that the base ten system is "handy" because—well, look for yourself:

But other base systems have been used over the years. Many ancient cultures used a base 20 system** (fingers and toes). In the vigesimal system, when you wrote **35**, that meant 3 score + 5 ones. A **score** means 20. So **35** in the base 20 system is the same as 65 in the base ten system.

Traces of the vigesimal system remain in President Lincoln's famous words, "Four score and seven years ago. . . ."

It's time to take a little break. It's time for *Your Turn to Play*. I've been having all the fun so far. It's only fair that you get your chance.

The answers are listed right after all the questions, but please play with the questions a little bit (that is, answer them in writing) before you look at the answers.

[★] In fancy language, we call this a **place-value system** or, even fancier, a **positional numeration system**.

^{**} More fancy language: vigesimal numeration system [vy JESH eh mul].

Your Turn to Play

- 1. Write 87 in the vigesimal system.
- 2. Another really popular numeration system was the base 12 (duodecimal system). There are lots of places in everyday life that reflect the old base 12 system. Can you name three?
- 3. The oldest known place value system is the Babylonian sexagesimal system (base 60). Can you think of a couple of places in everyday life today that reflect that old

system?

$$4. \ 4 \frac{2}{3} - 2 \frac{3}{4} = ?$$

......COMPLETE SOLUTIONS......

- 1. 87 = 4 score + 7 = 47.
- 2. Look at a clock (12 hours). Look at a calendar (12 months). Look at a ruler (12 inches). Look at a jury (12 people). Look at eggs (dozen). Look at gold (12 troy ounces = 1 pound).
- 3. Did you ever wonder why there are sixty seconds in a minute, and sixty minutes in an hour? Now you know. In geometry we will study angles. A one-degree angle (written 1°) is very small. It takes 90 of them to make a right angle.



If you get out your microscope, and picture splitting a one-degree angle into 60 angles, each of those is called a minute. Sixty minutes of angle equals one degree. If you take an angle that measures one minute and split it into 60 little angles, each of those would measure one second. These are super tiny angles.

$$4. \ 4\frac{2}{3} - 2\frac{3}{4} = 4\frac{8}{12} - 2\frac{9}{12} = 3\frac{12}{12} + \frac{8}{12} - 2\frac{9}{12} = 1\frac{11}{12}$$

Index

	corollary
	counting numbers
≈	crepuscular perambulation 97
€	d = rt
\cap	decimals
U	
	adding
<i>≠</i>	multiplying
Ø 50	repeating
≐	subtracting
.50¢99	terminating
A Man Called Peter 162	diameter
A – B (subtraction of sets) 52	difference between two sets 52
adding decimals	discount
alliteration	double and triple
altitude of a triangle 122	distance equals rate times time 113
ambrosia 83, 104, 109	dividend
angles in degrees and seconds 16, 63	divisibility
approximately equal to 26, 71	divisor
area of a circle	double-left rule
area of a parallelogram 129, 131	double-right rule
area of a rectangle 96, 118	elapsed time 159, 160
area of a triangle	elliptical statements 115
Babylonian sexagesimal system 16	empty set
bar graphs 79, 80	equals after rounding off ± 28
base ten	exponents
base twenty	f(x)
belongs to ∈ 47	first coordinate 146
big numbers	football at KITTENS University 94
billion	Forty-Sixth Rule of Robotics 46
braces	function
Briggs, Henry (inventor of long	definition
division) 156	graphs of a function 147, 148
$C = \pi d$	image
calculators banned 8	mapped
Cecil Rodd's famous advertising slogan	ordered pair
for Wall's ice cream 164	furlong
centimeter	gibbous moon53
Cheeses from A to C	Goldbach conjecture
circle graphs 101	first form 92
circumference	second form
composite numbers	good teaching–five rules
congruent triangles	graphing
consecutive numbers90	Heron's formula
conversion factor	heron—the bird
Conversion factor	neron the ond

Index

Heron-the man	Prof. Eldwood's Why Your Work is Not
homonyms 17, 61	Done When the Cows Mow
image	<i>Your Lawn 118</i>
inclusive	quadrillion
integers	quintillion
intersection of sets 51	quotient
inverse function 23, 39, 40, 121	radius
liberty vs. freedom 66	ratio
<i>Life of Bobbie</i> 50	five ways to write a ratio 140
litotes	rhetorical questions
mapped143	right angle
mea culpa	Rossetti, Christina
memorizing	rounding 27, 28
mental arithmetic	rules for cutting up meat
metaphor	rules of divisibility 53, 60
million	sea chanty 104, 109-111, 125
multiplying decimals	semiperimeter
natural numbers 62, 81, 89	set
negative numbers 146	definition 46
Newton, Isaac	difference between two sets 52
nine conversions	element of
open question in mathematics 93	empty set 50
ordered pair	member of
past tense of verbs	subset 48, 49
percent (definition)	when two sets are equal 49
perimeter	Ø
pi	set-builder notation
pie charts	square root 121, 122
place-value system	squaring a number 39, 76, 81, 121
positional numeration system 15	subtracting decimals
presbyopia	subtracting mixed units 43, 44
prime numbers 89	Ten Commandments 85
Prof. Eldwood's Algebra and Algebra	terminating decimals
Revisited, 11th edition 128	"The Night Has a Thousand Eyes" by
Prof. Eldwood's Financing Your Teepee	Francis William Bourdillion
with 119	
Prof. Eldwood's Flossing for the	theorem (definition) 108
Modern Man 160	trick of adding zeros 20, 65
Prof. Eldwood's Guide to Modern	trillion
<i>Ironing</i> 116	"Twilight Night" by Rossetti 149
Prof. Eldwood's Modern Clown Masks	union of sets
	verbs
Prof. Eldwood's Modern Tea Parties	vigesimal system
	whole numbers 14, 35, 62
Prof. Eldwood's The President Who	"Why We Do Mathematics"—an essay
Came Between 129	
Prof. Eldwood's When Bad Things	"Winter: My Secret" by Rossetti 124
Happen to Good Bugs 37	Wizard of Oz movie

Index

x-axis	148
x-coordinate	146
y-axis	148
y-coordinate	146
Young Hickory of the Granite Hills	
	129

To see what other books have been written about Fred please visit FredGauss.com