

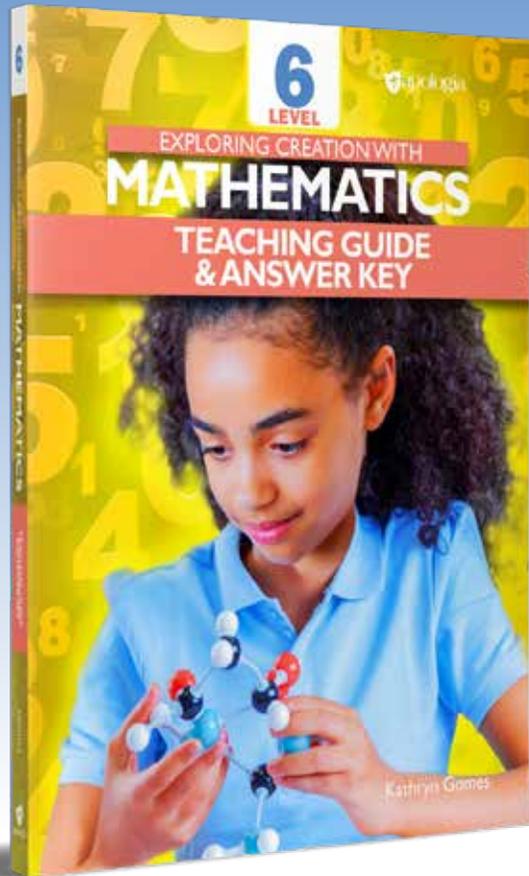
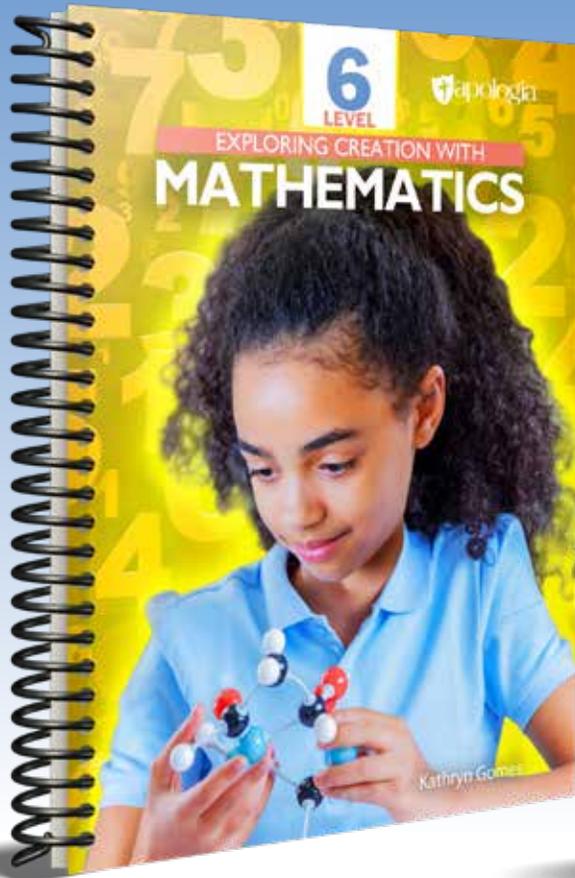
6  
LEVEL

apologia

EXPLORING CREATION WITH  
**MATHEMATICS**



Kathryn Gomes



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# WHOLE NUMBERS

**In this chapter, you will learn to:**

- Find multiples and factors
- Evaluate exponents
- Use the order of operations





## LESSON 1: MULTIPLES

### The Most Multiples

#### You Will Need:

- 2 players
- 2 different colored pencils
- Numbered cards 3–10 (such as Uno cards or playing cards)

#### You Will Do:

1. Shuffle the cards. Player One draws a card and colors in all the multiples of that number on the chart below. It is ok for players to skip count if they do not remember all of the multiples.
2. Player Two draws a card and colors in the multiples of that number. If a multiple is already colored in, it is skipped.
3. Play continues until all the numbered cards have been played. The player with the most squares colored in wins.



1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50

**Multiples** are the result of multiplying a number. For instance, the multiples of 7 are 7, 14, 21, 28, and on and on. There is no end to the number of multiples.

If a number is the multiple of two or more numbers, we call it a **common multiple**. Below is a list of the multiples of 4 and 5. The common multiples of 4 and 5 are circled.

Multiples of 4: 4, 8, 12, 16, 20, 24, 28, 32, 36, 40, 44, 48, ...

Multiples of 5: 5, 10, 15, 20, 25, 30, 35, 40, 45, 50, ...

Common multiples can help you solve many different kinds of problems. But, they are especially helpful when you try to add and subtract fractions with different denominators. You will learn more about that in Chapter 3.



**MULTIPLES:** The result of multiplying a number

**COMMON MULTIPLE:** When a number is a multiple of 2 or more numbers

**EXAMPLE 1: List the first 8 multiples of 8.**

We can skip count to find these or just do the multiplication in our head.

$$8 \times 1 = 8 \quad 8 \times 5 = 40$$

$$8 \times 2 = 16 \quad 8 \times 6 = 48$$

$$8 \times 3 = 24 \quad 8 \times 7 = 56$$

$$8 \times 4 = 32 \quad 8 \times 8 = 64$$

**EXAMPLE 2: Find a common multiple of 5 and 8.**

First, we will list the multiples of 5. Then, the multiples of 8. We will circle the numbers that are common on both lists.

Multiples of 5: 5, 10, 15, 20, 25, 30, 35, 40, 45, 50, ...

Multiples of 8: 8, 16, 24, 32, 40, 48, 56, 64, 72, ...

40 is a common multiple of 5 and 8.



**1. List the next 7 multiples for each number.**

a. 4, \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_

b. 7, \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_

c. 6, \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_

d. 9, \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_

e. 5, \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_

**2. Is 33 a multiple of 3? Yes or no?**

**3. Is 42 a multiple of 4? Yes or no?**

**4. List a common multiple of 4 and 7. \_\_\_\_\_**

**5. Look back at the multiples of 5 above. Circle any multiples of 5 that are also multiples of 3.**

**6. Give an example of a number that is a common multiple of 4 and 6. There is more than one correct answer.**

---

**7. At a certain store, hot dogs are only sold in packs of 10, and buns are only sold in bags of 8. What is the least number of hot dogs and buns you can buy so that there is one bun for each hot dog?**

---

**8. Mrs. Gong volunteers at the library every 6 days and Mr. Gong volunteers at the local theater every 7 days. How many days will it be before they are both volunteering on the same day?**

---

**WARM UP**

Use your knowledge of multiplication problems to fill in the blanks in each problem. It may take you a few guesses to find the right digit.

a.

$$\begin{array}{r} 3,214 \\ \times \quad \square \\ \hline 19,284 \end{array}$$

b.

$$\begin{array}{r} 4 \square \\ \times 38 \\ \hline 352 \\ + 1320 \\ \hline 1,672 \end{array}$$

When we multiply multi-digit numbers, we multiply the ones first and then continue from there. No matter how large the number is that you are multiplying, make sure you always start with the ones and work your way left.

Let's review several different kinds of multiplication problems.

**EXAMPLE 1: Find the product.**

$$\begin{array}{r} 2,329 \\ \times \quad 4 \\ \hline \end{array}$$

We are multiplying a 4-digit number by a 1-digit number. We just need to start with the ones place value.

$$\begin{array}{r} \phantom{0}^3 \\ 2329 \\ \times \quad 4 \\ \hline 6 \end{array}$$

Multiply the 4 by the 9 ones. This results in 36. We write the 6 ones place value below and the 3 above the tens column.

$$\begin{array}{r} \phantom{0}^1 \phantom{0}^{13} \\ 2,329 \\ \times \quad 4 \\ \hline 9,316 \end{array}$$

Multiply by the tens, hundreds, and thousands being careful to add on any regroupings.

A quick estimate helps us check to make sure our answer makes sense. Our answer should be close to, but less than, 10,000.

$$2500 \times 4 = 10,000$$

When we multiply a 2-digit by a 2-digit number, we need to pay very careful attention to place value.

**EXAMPLE 2: Find the product.**

$$\begin{array}{r} 35 \\ \times 42 \\ \hline \end{array}$$

$$\begin{array}{r} 1 \\ 35 \\ \times 42 \\ \hline 70 \end{array}$$

When multiplying the 2 by the 5 ones, we must regroup and write a 1 above the tens column. We add this to 6 tens and write a 7 below.

$$\begin{array}{r} 2 \\ 35 \\ \times 42 \\ \hline 70 \\ \hline 00 \end{array}$$

Before multiplying through by the 4 tens, we need to write a zero in the ones column. 4 tens times 5 is 200. We write the 0 and put the 2 above the tens column.

$$\begin{array}{r} 2 \\ 35 \\ \times 42 \\ \hline 70 \\ \hline + 1,400 \\ \hline 1,470 \end{array}$$

4 multiplied by 3 is 12. Add on the 2 to 12 to get 14. Finally, we add up the total.

A quick estimate helps us check to make sure our answer makes sense.

$$40 \times 40 = 1,600$$

**EXAMPLE 3:** Find the product.

$$\begin{array}{r} 2,049 \\ \times \underline{27} \end{array}$$

$$\begin{array}{r} \phantom{0}^{36} \\ 2,049 \\ \times \underline{27} \\ \hline 14,343 \end{array}$$

Multiply through by the 7 ones, and be careful with the regrouping.

$$\begin{array}{r} \phantom{0}^1 \\ 2,049 \\ \times \underline{27} \\ \hline 14,343 \\ + \underline{40,980} \end{array}$$

Before multiplying through by the tens, we need to write a zero in the ones column. Then we multiply the 2 by 9 to get 18. We write the 8 below in the tens column and the one above the hundreds column.

$$\begin{array}{r} 2,049 \\ \times \underline{27} \\ \hline 14,343 \\ + \underline{40,980} \\ \hline 55,323 \end{array}$$

Finally, we add up the total.

A quick estimate helps us check to make sure our answer makes sense.

$$2,000 \times 30 = 60,000$$

Physicists are scientists who study matter, energy, and time. They use multiplication in when finding the force of an object by multiplying the mass by the acceleration. They use this calculation for many things including putting a spacecraft into orbit.





Find each product. Write the letter in the box below with the same number to solve the riddle.

## WHAT DID THE SKELETON ORDER FOR DINNER?

$\overline{\quad}$      $\overline{\quad}$      $\overline{\quad}$      $\overline{\quad}$      $\overline{\quad}$                        $\overline{\quad}$      $\overline{\quad}$      $\overline{\quad}$      $\overline{\quad}$   
 350    3,699    297    900    20,410                      900    1,476    1,443    350

**P**    1,233  
       ×   3  
 -----

**E**    4,082  
       ×   5  
 -----

**B**        37  
       × 39  
 -----

**S**        14  
       × 25  
 -----

**S**        35  
       × 10  
 -----

**R**        25  
       × 36  
 -----

**A**        27  
       × 11  
 -----

**I**        82  
       × 18  
 -----

**R**        18  
       × 50  
 -----



## LESSON 3: FACTORS

### Fabulous Factors

#### You Will Need:

- 2 players
- 2 colored pencils

#### You Will Do:

1. Player One chooses any number on the board and circles it with his or her colored pencil.
2. Player Two circles all the factors of Player One's number that are on the board. For instance, if Player One circled 24, then Player Two would circle 1, 2, 3, 4, 6, 8, and 12.
3. Player Two chooses a number on the board and circles it.
4. Player One circles all the factors of Player Two's number that are still available on the board. Players can agree on a certain number of turns until the game is over. Or, they can play until all spaces are circled. The player with the most numbers circled wins.



1	2	3	4	5
6	7	8	9	10
11	12	13	14	15
16	17	18	19	20
21	22	23	24	25

A **factor** is a number that divides into another number, leaving no remainder. It is often helpful to find a factor of two numbers. The largest factor that two numbers share is called the **greatest common factor**.

Finding the factors of a number is an important skill that will help you solve many kinds of problems in the future. It can help you simplify fractions or start a long division problem.



**FACTOR:** A factor is a number that is multiplied to get a product. It also divides evenly into that product.

Example: The factors of 30 are 1, 2, 3, 5, 6, 10, 15, and 30. The factors of 25 are 1, 5, and 25.

**GREATEST COMMON FACTOR:** This is the largest factor that two numbers have in common.

Example: The greatest common factor of 25 and 30 is 5.

**EXAMPLE 1: Find all the factors of 24.**

The easiest way is to make a list of all the ways you can multiply two numbers to get 24. If we go in order, we can make sure we don't miss any.

$$1 \times 24$$

$$2 \times 12$$

$$3 \times 8$$

$$4 \times 6$$

$$5 \times ???$$

We cannot multiply 5 to get 24. And then we would be up to 6, which we already listed. We have a complete list.

Factors of 24: 1, 2, 3, 4, 6, 8, 12, 24

**EXAMPLE 2: What is the greatest common factor of 56 and 28?**

Start by listing the factors.

Factors of 28: 1, 2, 4, 7, 14, 28

Factors of 56: 1, 2, 4, 7, 8, 14, 28, 56

The greatest common factor is 28.

A **prime** number is a number with only one pair of factors. That pair of factors will always be 1 and the number itself. The prime numbers less than 10 are 2, 3, 5, and 7. It must be a pair of numbers, 1 and the number. This is why 1 is not prime, it only has one factor; itself!

If a number is greater than 1 and has more than one pair of factors, we say it is **composite**. The number 15 is a composite number.



**PRIME:** Any whole number greater than 1 is prime if its only factors are 1 and itself.

**COMPOSITE:** Any whole number greater than 1 that is not prime.

**EXAMPLE 3: List the factors of 23. Is 23 prime or composite?**

We will make a list.

$$1 \times 23 \qquad 6 \times \text{?????}$$

$$2 \times \text{????} \qquad 7 \times \text{?????}$$

$$3 \times \text{???} \qquad 8 \times \text{????}$$

$$4 \times \text{????} \qquad 9 \times \text{????}$$

$$5 \times \text{????} \qquad 10 \times \text{????}$$

We cannot multiply 2, 3, 4, 5, 6, 7, 8, 9 or 10 to get 23. At that point, we know we haven't skipped any factors.

Factors of 23: 1, 23

23 is prime.

**1. List the factors of each number.**

50

6

22

35

**2. Find the greatest common factor of each pair of numbers.**

a. 77 49	b. 99 88
c. 56 42	d. 64 48

**3. Find the factors of each number. Then, circle whether it is prime or composite.**

12

prime/composite

27

prime/composite

31

prime/composite

39

prime/composite

**WARM UP**

Prepare for today's lesson by making a list of all the prime numbers under 30. Use the list of numbers below to help you eliminate numbers that have more than two factors.

1. One is not prime. You can cross it out.
2. Any number other than 2 that has 2 as a factor is not prime. You can cross out all of these numbers on the list. This will mean that you are crossing out all of the even numbers except 2.
3. Any number other than 3 that has 3 as a factor is not prime. You can skip count by 3's to eliminate all of these numbers.
4. Any number other than 5 that has 5 as a factor is not prime. You can cross out all of these numbers on the list. They will all have a zero or a 5 as their ones digit.
5. Look at the remaining numbers. Do any of them have more than 2 factors? If so, cross them out.
6. The remaining numbers are a list of primes. Check your list against the one in the answer key.

<b>1</b>	<b>2</b>	<b>3</b>	<b>4</b>	<b>5</b>
<b>6</b>	<b>7</b>	<b>8</b>	<b>9</b>	<b>10</b>
<b>11</b>	<b>12</b>	<b>13</b>	<b>14</b>	<b>15</b>
<b>16</b>	<b>17</b>	<b>18</b>	<b>19</b>	<b>20</b>
<b>21</b>	<b>22</b>	<b>23</b>	<b>24</b>	<b>25</b>
<b>26</b>	<b>27</b>	<b>28</b>	<b>29</b>	<b>30</b>

Prime numbers under 30: \_\_\_\_\_

In the last lesson, you found pairs of factors for a number. In this lesson, you will find the **prime factorization** of a number. The prime factorization of a number is when we write a number only as the product of prime numbers. Below are examples of two prime factorizations.

$$30 = 2 \times 3 \times 5$$

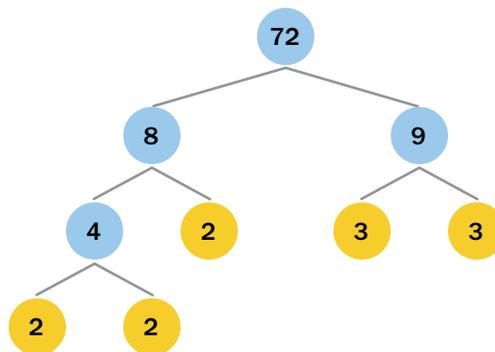
$$36 = 2 \times 2 \times 3 \times 3$$



### PRIME FACTORIZATION:

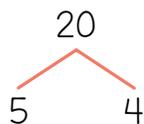
Rewriting the number as a product of prime numbers.

A tree diagram is a helpful way to find the prime factorization of a number.

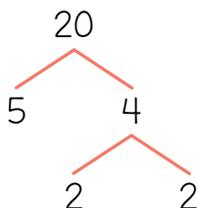


$$72 = \underline{2} \times \underline{2} \times \underline{2} \times \underline{3} \times \underline{3}$$

#### EXAMPLE 1: Find the prime factorization of 20.

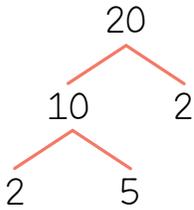


Begin by rewriting 20 as the product of 2 numbers. These two numbers will be the first branches of our tree.



The factor 5 is prime, so that branch of the tree is done. But, 4 is not prime. We will split it into two factors.

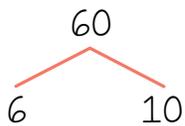
We know that 2 is prime. All of the branches of the tree are prime, so the tree is finished. Let's write out the product. When we do this, we always write the factors in order from least to greatest.  $20 = 2 \times 2 \times 5$



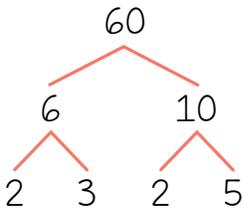
Note that if we had started with two different factors, we would still have arrived at the same answer. The order is different, but when we write the factors in order from least to greatest, we will see that it is the same answer.

$$20 = 2 \times 2 \times 5$$

**EXAMPLE 2:** Find the prime factorization of 60.



This is a larger number. But remember, you can start with any factor pair. Choose the factor pair that is the easiest for you.



Neither of the branches ends in a prime number. We will need to split both branches again into factor pairs.

Every branch ends in a prime number. We do not need to factor again. Now we need to write out the factors from least to greatest.  $60 = 2 \times 2 \times 3 \times 5$

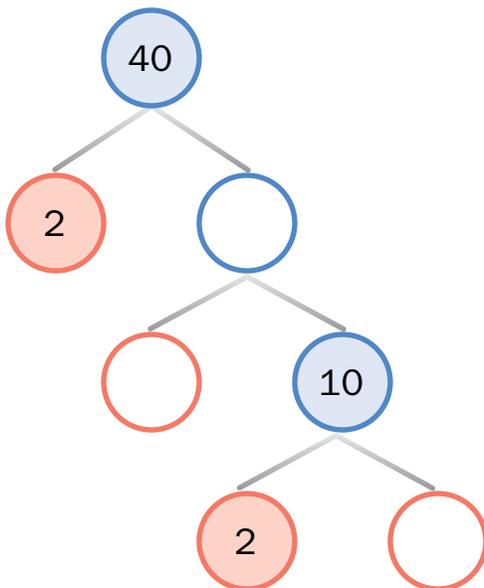


Prime numbers are very important in math and in life. They are used for many things including generating strong passwords for cyber security.



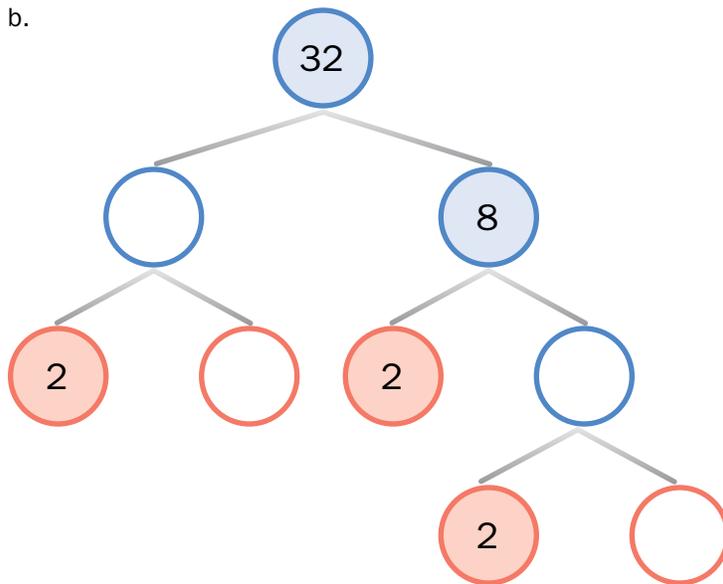
1. Fill in the missing numbers on each tree diagram. Then write out the prime factorization.

a.



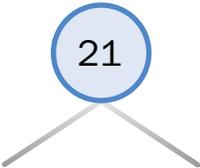
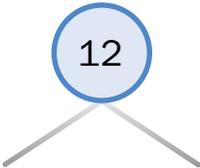
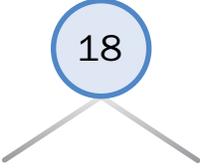
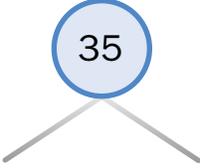
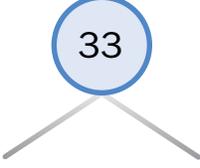
$40 = \underline{\quad} \times \underline{\quad} \times \underline{\quad} \times \underline{\quad}$

b.



$32 = \underline{\quad} \times \underline{\quad} \times \underline{\quad} \times \underline{\quad} \times \underline{\quad}$

2. Use tree diagrams to find the prime factorization of each number.

a. 	b. 
c. 	d. 
e. 	f. 

## ACTIVITY

## LESSON 5: LONG DIVISION (DAY ONE)

## Long Division Scramble

**You Will Need:**

- Lesson 5: Activity Sheet
- Scissors

**You Will Do:**

1. Carefully tear out the activity sheet from the back of the answer key. Cut the strips apart along the dashed lines.
2. Rearrange the strips to correctly show each long division problem. Have your parent check your answers.



In this lesson and the next, we will be reviewing long division. We use long division to systematically divide large numbers. Begin by reviewing the steps shown in the box to the right.

Because the problems are longer, some students have trouble remembering which step to do next. Remember that you continue to Divide, Multiply, Subtract, and Bring Down until you get to the end of the dividend.

**STEPS FOR LONG DIVISION**

<b>D</b>	÷	Divide
<b>M</b>	×	Multiply
<b>S</b>	−	Subtract
<b>B</b>	↓	Bring down

**EXAMPLE 1: Find the quotient.****D**

$$\begin{array}{r} 5 \\ 9 \overline{)504} \end{array}$$

Divide. We cannot divide 9 into 5. However, 9 goes into 50 five times. Write the 5 above the zero.

**M**

$$\begin{array}{r} 5 \\ 9 \overline{)504} \\ -45 \phantom{0} \\ \hline 5 \phantom{0} \end{array}$$

Multiply 9 by 5. The product is 45. Write that directly below and then subtract. There are 5 remaining.

**S**

B

$$\begin{array}{r} 5 \\ 9 \overline{)504} \\ - 45 \\ \hline 54 \end{array}$$

Bring down the 4.

$$\begin{array}{r} 56 \\ 9 \overline{)504} \\ - 45 \\ \hline 54 \\ - 54 \\ \hline 0 \end{array}$$

Divide 9 into 54. Nine goes into 54 six times. Write the 6 above the 4 in the ones column. Multiply and subtract. There is no remainder.

**EXAMPLE 2: Find the quotient.**

D

$$\begin{array}{r} 1 \\ 5 \overline{)86} \end{array}$$

Divide 5 into 8. It goes into 8 one time. Write the one above the 8.

M

$$\begin{array}{r} 1 \\ 5 \overline{)86} \\ - 5 \\ \hline 3 \end{array}$$

Multiply 5 by 1. Write the product below and subtract. There are 3 remaining.

S

$$\begin{array}{r} 1 \\ 5 \overline{)86} \\ - 5 \\ \hline 36 \end{array}$$

Bring down the 6.

B

$$\begin{array}{r} 17 \text{ r. } 1 \\ 5 \overline{)86} \\ - 5 \\ \hline 36 \\ - 35 \\ \hline 1 \end{array}$$

Divide 5 into 36. Five goes into 36 seven times. Multiply and subtract. There is a remainder of 1.

We can write the remainder using the letter “r” for remainder. Or, we can write the remainder as a fraction.

$$86 \div 5 = 17 \text{ r. } 1$$

$$86 \div 5 = 17 \frac{1}{5}$$

When we write a remainder as a fraction, the remainder is the numerator and the divisor is the denominator.



Find each quotient. For answers with remainders, write the answer with the “r.” notation and again as a fraction so you can practice both methods.

a.

$$6 \overline{)126}$$

b.

$$5 \overline{)650}$$

c.

$$8 \overline{)91}$$

d.

$$6 \overline{)27}$$

e.

$$4 \overline{)123}$$

f.

$$7 \overline{)145}$$

g.

$$9 \overline{)108}$$

h.

$$4 \overline{)323}$$

**WARM UP**

Today we will be using estimation to help us divide. Get ready for today's lesson by circling the number that is closest to each quotient below.

a.  $21\overline{)38}$   
1   3   5

b.  $16\overline{)33}$   
1   2   3

c.  $24\overline{)52}$   
1   2   3

d.  $15\overline{)85}$   
3   5   7

We will be practicing long division again in this lesson. The only difference is we will now solve problems with a two-digit divisor. We will follow the same four steps to do this: divide, multiply, subtract, and bring down.

When we divide in the first step, we will use estimation to help us decide how many times the divisor goes into the first part of our dividend. You also may need to do some multiplication on scratch paper on the side to check your estimate.

**EXAMPLE 1: Find the quotient.**

$$21\overline{)382}$$

**D**

$$\begin{array}{r} 1 \\ 21\overline{)382} \end{array}$$

Divide. We cannot divide 21 into 3. We need to estimate how many times it will divide into 38. We know that  $21 \times 2 = 42$ , which is too large. We will estimate that it goes into 38 one time.

**M**

$$\begin{array}{r} 1 \\ 21\overline{)382} \\ - 21 \\ \hline 17 \end{array}$$

Multiply  $1 \times 21$  and write the product below. Subtract. The difference is less than 21, so we now know that we divided correctly in the first step.

**S**

B

$$\begin{array}{r} 18 \\ 21 \overline{)382} \\ \underline{-21} \\ 172 \end{array}$$

Bring down the 2. We now need to divide 21 into 172. Again, we will use estimation. We know  $160 \div 20 = 8$ . We will estimate that 21 goes into 172 eight times.

$$\begin{array}{r} 18 \text{ r. } 4 \\ 21 \overline{)382} \\ \underline{-21} \\ 172 \\ \underline{-168} \\ 4 \end{array}$$

Multiply. The product of  $8 \times 21$  is 168. Write this below. Subtract. There are 4 remaining. We can write the remainder with the "r." notation.

We can also write the answer with a fraction.

$$18 \frac{4}{21}$$

Another strategy is to use multiples to help you divide. You'll want to make a list of the multiples of the divisor on the side or on a separate sheet of scratch paper. One advantage of this method is that you can use the same list many times for the same problem. Let's work through an example to see how this can help you.

### Common Mistake

If you do not divide correctly on the first step, you will have a difference that is larger than your divisor.

33 can still go 1 more time into 34. We did not divide correctly on the first step.

Since we used 1 to start, we need to go back and increase that number to a 2.

			1	
3	3	6	7	1
	-	3	3	
		3	4	

**EXAMPLE 2:** Find the quotient.

$$33 \overline{)671}$$

Before we start the long division steps, we will make a list of the multiples of 33.

$$33 \times 1 = 33$$

$$33 \times 2 = 66$$

$$33 \times 3 = 99$$

$$33 \times 4 = 132$$

**D**

$$\begin{array}{r} 2 \\ 33 \overline{)671} \end{array}$$

Divide. We cannot divide 33 into 6. We need to divide it into 67. Looking at our list of multiples, we can see that it will divide into 67 two times.

**M**

$$\begin{array}{r} 2 \\ 33 \overline{)671} \\ - 66 \\ \hline 1 \end{array}$$

Multiply  $2 \times 33$  and write the product below. Subtract. The difference is less than 33, so we now know that we divided correctly in the first step.

**S**

$$\begin{array}{r} 20 \\ 33 \overline{)671} \\ - 66 \\ \hline 11 \end{array}$$

Bring down the 1. We now need to divide 33 into 11. It is larger than 11, so we know it goes in zero times. Write the zero above.

**B**

$$\begin{array}{r} 20 \text{ r. } 11 \\ 33 \overline{)671} \\ - 66 \\ \hline 11 \\ - 0 \\ \hline 11 \end{array}$$

Multiply. The product will be zero. Write this below. Subtract. There are 11 remaining.

We can also write the answer using a fraction.

$$20 \frac{11}{33}$$

Simplified the answer will be:

$$20 \frac{1}{3}$$



1. Find each quotient. Use estimation to help you divide correctly.

a.  $16\overline{)339}$

b.  $15\overline{)852}$

c.  $22\overline{)375}$

2. Find each quotient. A list of multiples is provided to help you divide correctly.

a.  $24\overline{)679}$

$$24 \times 1 = 24$$

$$24 \times 2 = 48$$

$$24 \times 3 = 72$$

$$24 \times 4 = 96$$

b.  $13\overline{)5614}$

$$13 \times 1 = 13$$

$$13 \times 2 = 26$$

$$13 \times 3 = 39$$

$$13 \times 4 = 52$$

$$13 \times 5 = 65$$

$$13 \times 6 = 78$$

$$13 \times 7 = 91$$

3. Find each quotient. First, write out a list of the multiples on a separate sheet of paper and then divide.

a.  $15\overline{)467}$

b.  $22\overline{)875}$



## EXONENTS

### Exponent Exploration

#### You Will Need:

- Beans (or another small counter to act out the problem)
- Calculator

#### You Will Do:

1. Brandon's grandmother offers him two options for his Christmas present. In option 1, he can choose to receive \$30. In option 2, he can receive \$2 on the first day, \$4 on the second day, and \$8 on the third day, with the amount doubling each day for 10 days. Which option would you choose?



2. Act out the problem with your beans or another counter. Let each bean represent \$1. Write in the amount of money that Brandon would receive each day if he chooses option 2.

Day 1	Day 2	Day 3	Day 4	Day 5	Day 6	Day 7	Day 8	Day 9	Day 10
\$2	\$4	\$8							

3. Use your calculator to add up the total amount.

Total for Option 1: \$30

Total for Option 2: \_\_\_\_\_

You have already learned that you can use multiplication instead of doing repeated addition.

$$3 + 3 + 3 + 3 + 3 = 15 \quad \text{or} \quad 3 \times 5 = 15$$

But what about repeated multiplication? In the opening activity, the amount of money was multiplied by 2 each day. You could find the amount for the tenth day by multiplying by 2 ten times.

$$2 \times 2 \times 2$$

We can write repeated multiplication like this using a base and exponent. A base is the number we are multiplying, and the exponent shows us the number of times we will multiply the base by itself. We write the exponent up and to the right of the base and in a smaller size.

BASE →
2
←
EXPONENT
<sup>10</sup>



**BASE:** The number we are multiplying by itself.

**EXPONENT:** The number that shows us how many times we need to multiply the base by itself.

We can also use exponents for an expression that has two different bases.

**EXAMPLE 1:** Write the expression using exponents.  $4 \times 4 \times 4 =$

The base is 4 and the exponent is 3.

$$4^3$$

**EXAMPLE 2:** Write the expression using exponents.  $3 \times 3 \times 6 \times 6 \times 6 =$

We will use 2 different bases and 2 different exponents to write this expression.

$$3^2 \times 6^3$$

**EXAMPLE 3:** Use your calculator to find the correct exponent.  $5^{\square} = 125$

We could make a list and use a calculator to check.

$$5^1 = 5$$

$$5^2 = 5 \times 5 = 25$$

$$5^3 = 5 \times 5 \times 5 = 125$$

The exponent is 3.

**1. Write the expression using exponents.**

a.  $3 \times 3 \times 3 =$  \_\_\_\_\_

b.  $6 \times 6 \times 6 \times 6 =$  \_\_\_\_\_

c.  $8 \times 8 \times 8 \times 8 \times 8 =$  \_\_\_\_\_

d.  $10 \times 10 =$  \_\_\_\_\_

e.  $5 \times 5 \times 5 \times 6 \times 6 =$  \_\_\_\_\_

**2. Write out the expression using repeated multiplication.**

a.  $7^3$  \_\_\_\_\_

b.  $2^3$  \_\_\_\_\_

c.  $5^6$  \_\_\_\_\_

d.  $4^3 \times 2^5$  \_\_\_\_\_

**3. Use your calculator to find the missing exponent for each equation.**

a.  $2^{\square} = 32$

b.  $6^{\square} = 1,296$

c.  $3^{\square} = 243$

d.  $4^{\square} = 256$



## LESSON 8: SQUARES AND SQUARE ROOTS

### Square Number Bingo

#### You Will Need:

- A pair of dice
- 2 players
- 2 colored pencils

#### You Will Do:

1. Player One rolls the dice and adds the numbers to get a result between 2 and 12. They then multiply the number by itself. For instance, if a 1 and 4 is rolled, then multiply  $5 \times 5$  to get 25. Player One shades in any space with that product on the board below.
2. Player Two rolls and shades as well. If there is no available space to shade, then the turn is skipped.
3. The first player to get five spaces in a row vertically, horizontally, or diagonally wins. If no one gets 5 proper spaces, the one with the most colored spaces wins.



64	4	36	64	49
36	121	9	25	36
25	16	49	36	25
121	100	81	64	49
100	144	16	9	36

If you multiply a number by itself, the product is called a **square number**. The products are all amounts that can be formed into a square. These numbers can also be called **perfect squares**.



**SQUARE NUMBER:**

The result of multiplying a number by itself. Another name for these numbers is **PERFECT SQUARES**.

Square Numbers					
$1 \times 1 = 1$	$2 \times 2 = 4$	$3 \times 3 = 9$	$4 \times 4 = 16$	$5 \times 5 = 25$	$6 \times 6 = 36$
●	●● ●●	●●● ●●● ●●●	●●●● ●●●● ●●●● ●●●●	●●●●● ●●●●● ●●●●● ●●●●● ●●●●●	●●●●●● ●●●●●● ●●●●●● ●●●●●● ●●●●●● ●●●●●●

We can also use exponents when we square numbers. The expression  $3^2$  is read as *3 squared* or *3 to the 2nd power* and the expression  $4^3$  is read as *4 cubed* or *4 to the 3rd power*.

$$3 \times 3 = 3^2 = 9$$

**EXAMPLE 1:** Find each square number.

$4^2 =$

$10^2 =$

$7^2 =$

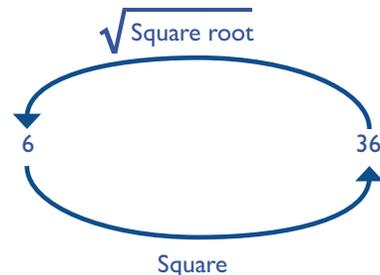
Write out each expression as repeated multiplication. Then, find the product.

$4^2 = 4 \times 4 = 16$

$10^2 = 10 \times 10 = 100$

$7^2 = 7 \times 7 = 49$

The opposite of squaring a number is finding the **square root**. When we find a square root, we ask ourselves, “What number could I square to get this product?” The symbol for square root is unique. It looks a bit like the long division symbol, but has a small check mark at the bottom.



**SQUARE ROOT:** the number that can be multiplied by itself to give the original number. For example, the square root of 36 is 6, because  $6 \times 6 = 36$ . The symbol for square root is  $\sqrt{\quad}$ .

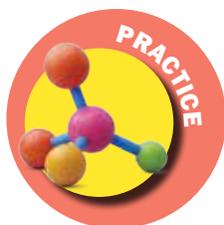
The square root of 81 is 9, because if we square 9 (multiplying 9 by itself) we will get 81.

**EXAMPLE 2:** Find the square root of each number.

$$\sqrt{4} = \quad \sqrt{49} = \quad \sqrt{64} =$$

We need to think of what number we can square to get each of the results that are under the square root sign.

$$\sqrt{4} = 2 \quad \sqrt{49} = 7 \quad \sqrt{64} = 8$$



**1. Square each of the numbers below.**

a.  $8^2$  \_\_\_\_\_

b.  $11^2$  \_\_\_\_\_

c.  $6^2$  \_\_\_\_\_

d.  $13^2$  \_\_\_\_\_

**2. Find each square root.**

a.  $\sqrt{9} =$  \_\_\_\_\_

b.  $\sqrt{1} =$  \_\_\_\_\_

c.  $\sqrt{81} =$  \_\_\_\_\_

d.  $\sqrt{25} =$  \_\_\_\_\_

e.  $\sqrt{100} =$  \_\_\_\_\_

f.  $\sqrt{169} =$  \_\_\_\_\_

g.  $\sqrt{4} =$  \_\_\_\_\_

h.  $\sqrt{16} =$  \_\_\_\_\_

3. A square tile has a side length of 9 inches. What is the area of the tile in square inches?
  
  
  
  
  
  
  
  
  
  
4. The area of a square garden is 25 square feet. What is the length of one side of the garden?
  
  
  
  
  
  
  
  
  
  
5. A square blanket has an area of 36 square feet. What is the length of one side of the blanket?

**CHALLENGE!**

Two square numbers have a sum of 25. What are the two numbers?



## LESSON 9: THE ORDER OF OPERATIONS (DAY ONE)

### Order of Operations Foldable

#### You Will Need:

- Lesson 9: Activity Sheet
- Scissors
- Colored pencils

#### You Will Do:

1. Carefully tear the activity sheet out of the back of the answer key and cut along the dashed lines. Cut slits on the smaller dashed lines and fold along the solid lines so that the images show on the outside and the large letters are on top of the step descriptions.
2. Color in the arrows above the “multiplication and division” and “addition and subtraction” steps. This is to remind you to always work from left to right.
3. Draw in parentheses and brackets on the top right flap.
4. Write two more examples of exponents on the exponents flap.
5. Look at the large letters on the top of your foldable. They spell *PEMDAS*. This acronym is one way students remember the order of operations.
6. You will fill in the inside of the foldable after reading today’s lesson.



The **order of operations** is an agreed upon order mathematicians use when working on problems. They created the order to make sure all mathematicians arrive at the same answer every time. You have worked with 3 steps of the order of operations before, but now you will learn the entire order.

#### The Order of Operations

1. Perform operations that are in grouping symbols.
2. Evaluate exponents.
3. Multiply and Divide (from left to right).
4. Add and Subtract (from left to right).



#### THE ORDER OF OPERATIONS:

This is an agreed upon order for doing math problems.

**EXAMPLE 1: Evaluate the expression.  $20 - 10 \div 2$** 

$20 - 10 \div 2$

There are no parentheses or exponents. We can skip the first step. We now need to multiply or divide from left to right. There is no multiplication. We need to divide.  $10 \div 2 = 5$

$20 - 5$

Now we do addition and subtraction from left to right. There is no addition. We need to subtract.

$15$

We have arrived at an answer that all mathematicians would agree to. Do you see how this is different from  $20 - 10 = 10$  then  $10 \div 2 = 5$ . Mathematicians must agree on the order to always arrive at the same answer!

**EXAMPLE 2: Evaluate the expression.  $3 \times 5^2 + 4 \times (2 + 4)$** 

$3 \times 5^2 + 4 \times 6$

Our first step is to do whatever is inside of grouping symbols. In this example we have parentheses.  $2 + 4 = 6$

$3 \times 25 + 4 \times 6$

Next, we need to evaluate the exponent.  $5^2 = 5 \times 5 = 25$

$75 + 24$

Now, we multiply (or divide) working from left to right.  
 $3 \times 25 = 75$  and  $4 \times 6 = 24$

$99$

Finally, we add (or subtract) working from left to right.  
 $75 + 24 = 99$

**EXAMPLE 3: Evaluate the expression.  $3 + (4^2 - 10)$** 

$3 + (16 - 10)$

Our first step is to do whatever is inside of the parentheses. There are two operations. When this happens you start again at the beginning of the order of operations. There are no more grouping symbols so we will evaluate the exponent first. Now, we subtract within the parentheses.  $16 - 10 = 6$

$3 + 6$

Finally, we evaluate this problem and see we need to add to get the final answer.  $3 + 6 = 9$

Fill in the inside of your foldable following the order of operations shown in the above examples.



Evaluate each expression. Remember to use PEMDAS through each stage of solving. Look at your foldable if you need help remembering the steps.

a.  $5 + 21 \div 3 \times 2$

b.  $9 + (62 - 12)$

c.  $33 \div (15 - 4) + 3$

d.  $(7 + 42) - 2 \times 3$

e.  $16 + 12 \div 4 - 2^2$

f.  $81 \div 3^2$

g.  $10^2 - 60 \div 6$

h.  $4 \times 5^2 + (3 + 2)$

**WARM UP**

The first letter of each step in the order of operations is written below. Do your best to write in the name of each step. Then, use your foldable from the last lesson to fill in any steps you forgot.

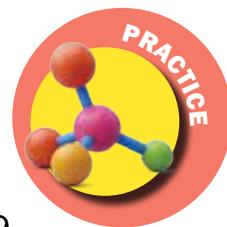
P\_\_\_\_\_

E\_\_\_\_\_

M/D\_\_\_\_\_ / \_\_\_\_\_

A/S\_\_\_\_\_ / \_\_\_\_\_

1. Evaluate each expression. Use your foldable to help you remember the steps.



a.  $5 \times (5 + 1) - 7$

b.  $(8 + 2^2) \div 3 + 9$

c.  $4 \times 3 + (9 - 9) + 3^2$

d.  $20 + 10 \div 2 - 3^2$

e.  $21 \div (15 - 8) + 10$

f.  $64 \div (2^2 + 4)$

**WARM UP**

Evaluate each expression.

a.  $10^2 + (12 \div 4)$

b.  $64 \div 4^2$

The **Distributive Property** states that multiplying a number by a group of numbers added together is the same as doing each multiplication separately. It can help us do many math problems mentally. It will also be essential in helping you do more complicated math in the future. Master breaking down simple problems now and becoming comfortable with it so that eventually it becomes second nature to you. Let's see why the property works.

$$10 \times (3 + 2) = 10 \times 5 = 50$$

$$10 \times 3 + 10 \times 2 = 30 + 20 = 50$$

**THE DISTRIBUTIVE PROPERTY:**

Multiplying a number by a group of numbers added together is the same as doing each multiplication separately.

**EXAMPLE 1:** Find the product of  $7 \times 56$  mentally.

Start by breaking the number 56 apart. We can do this by putting the addition inside parentheses.

$$7 \times 56$$

$$7 \times (50 + 6)$$

$$7 \times 50 + 7 \times 6$$

To multiply 7 times 50, think of  $7 \times 5$ , and then add a zero on the end.

$$350 + 42 = 392$$



Rewrite each multiplication problem by breaking the second factor apart. Then multiply mentally by using the Distributive Property.

a.  $5 \times 46$

$5 \times ( \quad + \quad )$

b.  $6 \times 34$

$6 \times ( \quad + \quad )$

c.  $3 \times 23$

$3 \times ( \quad + \quad )$

d.  $8 \times 41$

$8 \times ( \quad + \quad )$

e.  $7 \times 31$

$7 \times ( \quad + \quad )$

f.  $9 \times 33$

$9 \times ( \quad + \quad )$

g.  $10 \times 45$

$10 \times ( \quad + \quad )$

h.  $7 \times 52$

$7 \times ( \quad + \quad )$

**SKILLS CHECK**

You have been working with multiples and factors as part of the Unit 1 skills practice. Here are a few more for you to try.

1. List the next 5 multiples of each number.

a. 4, 8, \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_

b. 7, 14, \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_

2. Find all the factors of the given number.

a. 24 \_\_\_\_\_

b. 35 \_\_\_\_\_

3. Find each product or quotient.

a. 
$$\begin{array}{r} 4,516 \\ \times \quad 3 \\ \hline \end{array}$$

b.  $4 \overline{)23}$

c. 
$$\begin{array}{r} 34 \\ \times 27 \\ \hline \end{array}$$

d.  $24 \overline{)491}$

4. Evaluate each expression.

a.  $9 \div 3 + 2 =$

b.  $4^2 - 9 + 6 =$

5. Use mental math to find the product.

$4 \times 83$

6

LEVEL

apologia.

EXPLORING CREATION WITH

# MATHEMATICS

TEACHING GUIDE  
& ANSWER KEY



Kathryn Gomes

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# WEEK-BY-WEEK DAILY SCHEDULE

Below is a suggested weekly schedule to help you stay on track. It uses a four-day week to leave room for a co-op day or a review day. This schedule covers 36 weeks, but we encourage you to adjust it to the needs of your child and your family's calendar.

Week	Day 1	Day 2	Day 3	Day 4
<b>1</b>	<b>UNIT 1 INTRO</b> <input type="checkbox"/> <b>CHAPTER 1</b> <b>Lesson 1</b> Skills practice: multiples and factors	<b>CHAPTER 1</b> <input type="checkbox"/> <b>Lesson 2</b> Skills practice: multiples and factors	<b>CHAPTER 1</b> <input type="checkbox"/> <b>Lesson 3</b> Skills practice: multiples and factors	<b>CHAPTER 1</b> <input type="checkbox"/> <b>Lesson 4</b> Skills practice: multiples and factors
<b>2</b>	<b>CHAPTER 1</b> <input type="checkbox"/> <b>Lesson 5</b> Skills practice: multiples and factors	<b>CHAPTER 1</b> <input type="checkbox"/> <b>Lesson 6</b> Skills practice: multiples and factors	<b>CHAPTER 1</b> <input type="checkbox"/> <b>Lesson 7</b> Skills practice: multiples and factors	<b>CHAPTER 1</b> <input type="checkbox"/> <b>Lesson 8</b> Skills practice: multiples and factors
<b>3</b>	<b>CHAPTER 1</b> <input type="checkbox"/> <b>Lesson 9</b> Skills practice: multiples and factors	<b>CHAPTER 1</b> <input type="checkbox"/> <b>Lesson 10</b> Skills practice: multiples and factors	<b>CHAPTER 1</b> <input type="checkbox"/> <b>Lesson 11</b> Skills practice: multiples and factors	<b>CHAPTER 1</b> <input type="checkbox"/> <b>Chapter Review</b>
<b>4</b>	<b>CHAPTER 2</b> <input type="checkbox"/> <b>Lesson 12</b> Skills practice: long division	<b>CHAPTER 2</b> <input type="checkbox"/> <b>Lesson 13</b> Skills practice: long division	<b>CHAPTER 2</b> <input type="checkbox"/> <b>Lesson 14</b> Skills practice: long division	<b>CHAPTER 2</b> <input type="checkbox"/> <b>Lesson 15</b> Skills practice: long division



## TEACHER'S NOTES

# UNIT 1: WHOLE NUMBERS, DECIMALS, AND FRACTIONS

Unit One moves through a broad range of topics. Much of the content was introduced in previous Math Levels 4 and 5, but all kids need the review and reinforcement. And in some cases, more challenging problems are added in, like with the mixed number lessons. This unit lays the foundation for the rest of the year and for much of middle school-level mathematics.

### SUPPLY LIST

#### Skills Practice:

- Colored pencils
- Numbered cards 3-10 (such as Uno® cards or playing cards)
- Notecards
- Factor table worksheets (available on the Book Extras website)
- Long division worksheets (available on the Book Extras website)
- Prime factorization worksheets (available on the Book Extras website)

#### Chapter One:

- 2 players
- Colored pencils
- Numbered cards 3-10
- Scissors
- Beans (or another small counter)
- Calculator
- Dice
- Glue

#### Chapter Two:

- Scissors
- Game pieces
- 2 or more players
- Scratch paper
- A takeout menu
- A calculator

#### Chapter Three:

- Scissors
- 2 players
- An envelope
- Dominoes
- 2 players
- 2 different colored counters (this can be snacks or small game pieces)
- Dice
- Fraction tiles
- Graham crackers
- A recipe
- Markers

# SKILLS PRACTICE FOR UNIT ONE: WHOLE NUMBER OPERATIONS

As mentioned at the beginning of this book, the skills practice reviews skills that have already been introduced in this book. There is one exception, and that is the Unit One skills practice. The skills reviewed here were covered in previous levels of Exploring Creation with Mathematics. If you are switching programs, it is possible you haven't covered this material before. You may find the pace of the review is too quick for your child. Please adjust the pacing. These concepts are very important, and it would be better to review them thoroughly than just push forward.

## Skill One: Multiples and Factors

I cannot overemphasize the importance of students grasping multiples and factors. These concepts are interwoven through so much of mathematics. Polish this skill before students need to use them, such as when they work with fractions in Chapter 3.

1. Play “The Most Multiples” from Lesson 1. You can print additional game boards from the Book Extras website.
2. Print factor table worksheets off the Book Extras website.
3. Choose a number between 1 and 10, and have your child skip count to list all the multiples. This is just a quick activity that can be done verbally before starting the lesson for that day. Most students at this level will mainly need to focus on 4's, 6's, 7's, and 8's. Target the fact families your child seems to struggle with.

## Skill Two: Long Division

Long division takes time to master. It also can be very taxing because it is such a long process. That is why I think long division is a perfect skill for the skills practice. Give your child one quick problem or activity each day. Spreading it out ensures they will master it without overwhelming them with an entire page of long division problems.

1. Notecard problems. This is one of my favorite ways to do the skills practice when the skill itself is pretty taxing. I just write out one problem on a notecard or post-it. Have your child do that one problem before starting the lesson. Here are problems you can use. There are enough for the whole skills practice.

$$\begin{array}{r} 96 \\ 9 \overline{)864} \end{array}$$

$$\begin{array}{r} 99 \\ 5 \overline{)495} \end{array}$$

$$\begin{array}{r} 85 \\ 4 \overline{)340} \end{array}$$

$$\begin{array}{r} 59 \text{ r. } 3 \\ 6 \overline{)357} \end{array}$$

$$\begin{array}{r} 19 \text{ r. } 1 \\ 9 \overline{)172} \end{array}$$

$$\begin{array}{r} 11 \text{ r. } 5 \\ 16 \overline{)181} \end{array}$$

$$\begin{array}{r} 14 \text{ r. } 3 \\ 15 \overline{)213} \end{array}$$

$$\begin{array}{r} 10 \text{ r. } 8 \\ 12 \overline{)128} \end{array}$$

$$\begin{array}{r} 10 \text{ r. } 46 \\ 51 \overline{)556} \end{array}$$

2. There are long division worksheets available on the Book Extras website.
3. Find the missing digit puzzles. These are available on the Book Extras website. Instead of solving an entire long division problem, students just need to fill in the missing digits. It helps reinforce the steps of the process in a way that is less challenging.

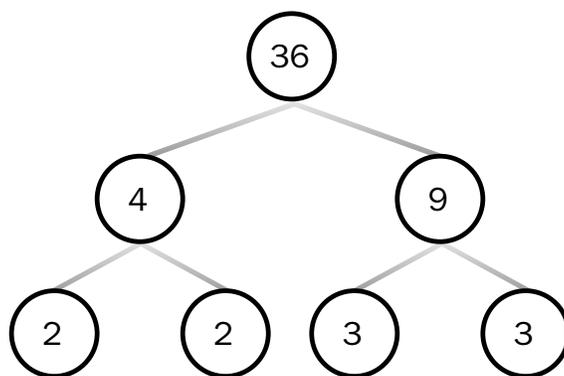
### Skill Three: Prime Numbers and Prime Factorization

Knowing the prime numbers up to 100 is a huge advantage for students. Minimally, they should know all of them up to 25. And prime factorization is a skill that takes some practice before it becomes automatic.

1. Have your child recite the prime numbers up to 100 (or 25) to you. The list is below so you can quickly check, or they can self-check. Consider offering them a prize if they can recite or write all the prime numbers under 100 by the end of the unit.

2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97

2. Have your child choose any number under 100 and write out the prime factorization. They can check their answer by multiplying on a calculator. There is an example below.



$$36 = 2 \times 2 \times 3 \times 3$$

3. There are prime factorization worksheets on the Book Extras website.

# CHAPTER 1: WHOLE NUMBERS, DECIMALS, AND FRACTIONS

## LESSON 1

This lesson is probably review for your student. It is helpful to have a gentle entry into a new level of mathematics. Multiples are foundational for finding the common denominator in future fraction lessons. There are additional copies of the game board on the Book Extras website so that you can play this game as part of the skills practice.

### Page 16 Answers

The screenshot shows a worksheet titled "LESSON 1 MULTIPLES" with a globe icon. It contains the following problems and answers:

- 1. List the next 7 multiples for each number.
  - a. 4, 8 12 16 20 24 28 32
  - b. 7, 14 21 28 35 42 49 56
  - c. 12 18 24 30 36 42 48
  - d. 18 27 36 45 54 63 72
  - e. 5, 10 15 20 25 30 35 40
- 2. Is 33 a multiple of 3? Yes or no?
- 3. Is 42 a multiple of 4? Yes or no?
- 4. List a common multiple of 4 and 7. Sample answer: 28
- 5. Look back at the multiples of 5 above. Circle any multiples of 5 that are also multiples of 3.
- 6. Give an example of a number that is a common multiple of 4 and 6. There is more than one correct answer.  
Possible sample answers: 12, 24, 36, 48
- 7. At a certain store, hot dogs are only sold in packs of 10, and buns are only sold in bags of 8. What is the least number of hot dogs and buns you can buy so that there is one bun for each hot dog?  
40 hot dogs and 40 buns
- 8. Mrs. Gong volunteers at the library every 6 days and Mr. Gong volunteers at the local theater every 7 days. How many days will it be before they are both volunteering on the same day?  
42 days

16

## LESSON 2

When students make mistakes in multi-digit multiplication, they often make the mistake repeatedly. Common mistakes include mixing up the regrouping and not realizing they are multiplying by a number in the tens place. The code in the practice helps students catch mistakes before they do the entire page incorrectly. You also might want to let your child check his or her work with a calculator.

Page 17 Answers

MULTIPLICATION LESSON 2

**WARM UP**  
Use your knowledge of multiplication problems to fill in the blanks in each problem. It may take you a few guesses to find the right digit.

a. 
$$\begin{array}{r} 3,214 \\ \times \quad 6 \\ \hline 19,284 \end{array}$$

b. 
$$\begin{array}{r} 4 \quad 4 \\ \times 38 \\ \hline 352 \\ + 1320 \\ \hline 1,672 \end{array}$$

When we multiply multi-digit numbers, we multiply the ones first and then continue from them. No matter how large the number is that you are multiplying, make sure you always start with the ones and work your way left.

Let's review several different kinds of multiplication problems.

**EXAMPLE 1:** Find the product.

$$\begin{array}{r} 2,329 \\ \times \quad 4 \\ \hline \end{array}$$

We are multiplying a 4-digit number by a 1-digit number. We just need to start with the ones place value.

$$\begin{array}{r} 2,329 \\ \times \quad 4 \\ \hline 9,316 \end{array}$$

Multiply the 4 by the 9 ones. This results in 36. We write the 6 ones place value below and the 3 above the tens column.

$$\begin{array}{r} 2,329 \\ \times \quad 4 \\ \hline 9,316 \end{array}$$

Multiply by the tens, hundreds, and thousands being careful to add on any regroupings.

A quick estimate helps us check to make sure our answer makes sense. Our answer should be close to, but less than, 10,000.  
 $2500 \times 4 = 10,000$

17

Page 20 Answers

LESSON 2 MULTIPLICATION

Find each product. Write the letter in the box below with the same number to solve the riddle.

**WHAT DID THE SKELETON ORDER FOR DINNER?**

S	P	A	R	E	R	I	B	S
360	3,699	287	900	20,410	900	1,476	1,443	360

P 
$$\begin{array}{r} 1,233 \\ \times \quad 3 \\ \hline 3,699 \end{array}$$

E 
$$\begin{array}{r} 4,082 \\ \times \quad 5 \\ \hline 20,410 \end{array}$$

B 
$$\begin{array}{r} 37 \\ \times 39 \\ \hline 333 \\ + 1,110 \\ \hline 1,443 \end{array}$$

S 
$$\begin{array}{r} 14 \\ \times 20 \\ \hline 280 \\ + 280 \\ \hline 350 \end{array}$$

S 
$$\begin{array}{r} 35 \\ \times 10 \\ \hline 350 \end{array}$$

R 
$$\begin{array}{r} 25 \\ \times 36 \\ \hline 150 \\ + 750 \\ \hline 900 \end{array}$$

A 
$$\begin{array}{r} 27 \\ \times 11 \\ \hline 27 \\ + 270 \\ \hline 297 \end{array}$$

I 
$$\begin{array}{r} 82 \\ \times 18 \\ \hline 656 \\ + 820 \\ \hline 1,476 \end{array}$$

R 
$$\begin{array}{r} 18 \\ \times 50 \\ \hline 00 \\ + 900 \\ \hline 900 \end{array}$$

20

LESSON 3

Factors are so essential in mathematics. Students will continue to review factors in the Unit 1 skills practice. This skill will be essential when they factor quadratics in high school. More immediately, they will need to be able to identify common factors when simplifying fractions.

Page 24 Answers

LESSON 3 FACTORS

1. List the factors of each number.

60	6	22	35
1 × 5 2 × 25 5 × 10 1, 2, 5, 10, 25, 50	1 × 6 2 × 3 1, 2, 3, 6	1 × 22 2 × 11 1, 2, 11, 22	1 × 35 5 × 7 1, 5, 7, 35

2. Find the greatest common factor of each pair of numbers.

a. 77: 1, 7, 11, 77	b. 99: 1, 3, 9, 11, 33, 99
49: 1, 7, 49	88: 1, 2, 4, 8, 11, 22, 44, 88
c. 56: 1, 2, 4, 7, 8, 14, 28, 56	d. 64: 1, 2, 4, 8, 16, 32, 64
42: 1, 2, 3, 6, 7, 14, 21, 42	48: 1, 2, 4, 6, 8, 12, 24, 48

3. Find the factors of each number. Then, circle whether it is prime or composite.

12: prime/composite	27: prime/composite
1 × 12    3 × 4 2 × 6 1, 2, 3, 4, 6, 12	1 × 27 3 × 9 1, 3, 9, 27
31: prime/composite	39: prime/composite
1 × 31	1 × 39 3 × 13 1, 3, 13, 39

24

## LESSON 4

Some students will really prefer this method of factoring to what we did in the previous lesson. The beauty of it is that you can split the number in many different ways and still arrive at the correct answer. All of the work with primes will also help them start to identify prime numbers more quickly.

### Page 25 Answers

PRIME FACTORIZATION LESSON 4

**WARM UP**  
Prepare for today's lesson by making a list of all the prime numbers under 30. Use the list of numbers below to help you eliminate numbers that have more than two factors.

- One is not prime. You can cross it out.
- Any number other than 2 that has 2 as a factor is not prime. You can cross out all of these numbers on the list. This will mean that you are crossing out all of the even numbers except 2.
- Any number other than 3 that has 3 as a factor is not prime. You can skip count by 3's to eliminate all of these numbers.
- Any number other than 5 that has 5 as a factor is not prime. You can cross out all of these numbers on the list. They will all have a zero or a 5 as their ones digit.
- Look at the remaining numbers. Do any of them have more than 2 factors? If so, cross them out.
- The remaining numbers are a list of primes. Check your list against the one in the answer key.

<del>1</del>	2	3	<del>4</del>	5
<del>6</del>	7	<del>8</del>	<del>9</del>	<del>10</del>
11	<del>12</del>	13	<del>14</del>	<del>15</del>
<del>16</del>	17	<del>18</del>	19	<del>20</del>
<del>21</del>	<del>22</del>	23	<del>24</del>	<del>25</del>
<del>26</del>	<del>27</del>	<del>28</del>	29	<del>30</del>

Prime numbers under 30: 2, 3, 5, 7, 11, 13, 17, 19, 23, 29

25

### Page 28 Answers

LESSON 4 PRIME FACTORIZATION

1. Fill in the missing numbers on each tree diagram. Then write out the prime factorization.

a.

```

    graph TD
      40((40)) --- 2((2))
      40 --- 20((20))
      20 --- 2((2))
      20 --- 10((10))
      10 --- 2((2))
      10 --- 5((5))
  
```

$40 = 2 \times 2 \times 2 \times 5$

b.

```

    graph TD
      32((32)) --- 4((4))
      32 --- 8((8))
      4 --- 2((2))
      4 --- 2((2))
      8 --- 2((2))
      8 --- 4((4))
      4 --- 2((2))
      4 --- 2((2))
  
```

$32 = 2 \times 2 \times 2 \times 2 \times 2$

28

### Page 29 Answers

PRIME FACTORIZATION LESSON 4

2. Use tree diagrams to find the prime factorization of each number.

a.

```

    graph TD
      21((21)) --- 3((3))
      21 --- 7((7))
  
```

$3 \times 7$

b.

```

    graph TD
      12((12)) --- 2((2))
      12 --- 6((6))
      6 --- 2((2))
      6 --- 3((3))
  
```

$2 \times 2 \times 3$

c.

```

    graph TD
      18((18)) --- 3((3))
      18 --- 6((6))
      6 --- 2((2))
      6 --- 3((3))
  
```

$2 \times 3 \times 3$

d.

```

    graph TD
      35((35)) --- 5((5))
      35 --- 7((7))
  
```

$5 \times 7$

e.

```

    graph TD
      24((24)) --- 4((4))
      24 --- 6((6))
      4 --- 2((2))
      4 --- 2((2))
      6 --- 2((2))
      6 --- 3((3))
  
```

$2 \times 2 \times 2 \times 3$

f.

```

    graph TD
      33((33)) --- 3((3))
      33 --- 11((11))
  
```

$3 \times 11$

29

# LESSON 5

Students have seen long division before in previous levels. But it is very common for students to struggle to remember all of the steps, or to just get rusty on the process after a break. This first lesson only uses one-digit divisors.

## Activity Sheet Answers

**LONG DIVISION SCRAMBLE**

**PROBLEM 1**

$$\begin{array}{r} 22 \\ 6 \overline{)132} \\ \underline{-12} \phantom{0} \\ 12 \\ \underline{-12} \\ 0 \end{array}$$

**PROBLEM 2**

$$\begin{array}{r} 52 \\ 5 \overline{)263} \\ \underline{-25} \phantom{0} \\ 13 \\ \underline{-10} \\ 3 \end{array}$$

**PROBLEM 3**

$$\begin{array}{r} 128 \\ 4 \overline{)515} \\ \underline{-4} \phantom{0} \\ 11 \\ \underline{-8} \phantom{0} \\ 35 \\ \underline{-32} \\ 3 \end{array}$$

**PROBLEM 4**

$$\begin{array}{r} 104 \\ 4 \overline{)417} \\ \underline{-4} \phantom{0} \\ 01 \\ \underline{-0} \\ 17 \\ \underline{-16} \\ 1 \end{array}$$

## Page 32 Answers

Find each quotient. For answers with remainders, write the answer with the "r" notation and again as a fraction so you can practice both methods.

a.  $\begin{array}{r} 21 \\ 6 \overline{)126} \\ \underline{-12} \\ 06 \\ \underline{-6} \\ 0 \end{array}$       b.  $\begin{array}{r} 130 \\ 5 \overline{)650} \\ \underline{-5} \phantom{0} \\ 15 \\ \underline{-15} \\ 00 \\ \underline{-0} \\ 0 \end{array}$

c.  $\begin{array}{r} 11 \text{ r.3} \\ 8 \overline{)91} \\ \underline{-8} \phantom{0} \\ 11 \\ \underline{-8} \\ 3 \end{array}$       d.  $\begin{array}{r} 4 \text{ r.3} \\ 6 \overline{)27} \\ \underline{-24} \\ 3 \end{array}$

$11 \frac{3}{8}$        $4 \frac{1}{2}$

e.  $\begin{array}{r} 30 \text{ r.3} \\ 4 \overline{)123} \\ \underline{-12} \\ 03 \\ \underline{-0} \\ 3 \end{array}$       f.  $\begin{array}{r} 20 \text{ r.5} \\ 7 \overline{)145} \\ \underline{-14} \\ 05 \\ \underline{-0} \\ 5 \end{array}$

$30 \frac{3}{4}$        $20 \frac{5}{7}$

g.  $\begin{array}{r} 12 \\ 9 \overline{)108} \\ \underline{-9} \phantom{0} \\ 18 \\ \underline{-18} \\ 0 \end{array}$       h.  $\begin{array}{r} 80 \text{ r.3} \\ 4 \overline{)323} \\ \underline{-32} \\ 03 \\ \underline{-0} \\ 3 \end{array}$

$80 \frac{3}{4}$

# LESSON 6

Now we are working with two-digit divisors. Estimation is going to be very key as we think about placing the first digit in the quotient.

## Page 33 Answers

**WARM UP**  
Today we will be using estimation to help us divide. Get ready for today's lesson by circling the number that is closest to each quotient below.

a.  $21 \overline{)38}$       b.  $16 \overline{)33}$   
 ① 3 5      1 ② 3

c.  $24 \overline{)52}$       d.  $15 \overline{)85}$   
 1 ② 3      3 ⑤ 7

We will be practicing long division again in this lesson. The only difference is we will now solve problems with a two-digit divisor. We will follow the same four steps to do this: divide, multiply, subtract, and bring down.

When we divide in the first step, we will use estimation to help us decide how many times the divisor goes into the first part of our dividend. You also may need to do some multiplication on scratch paper on the side to check your estimate.

**EXAMPLE 1:** Find the quotient.

$$\begin{array}{r} 1 \\ 21 \overline{)82} \\ \underline{-21} \\ 61 \end{array}$$

Divide. We cannot divide 21 into 8. We need to estimate how many times it will divide into 82. We know that  $21 \times 4 = 84$ , which is too large. We will estimate that it goes into 82 one time.

Multiply  $1 \times 21$  and write the product below. Subtract. The difference is less than 21, so we now know that we divided correctly in the first step.

33

## Page 36 Answers

1. Find each quotient. Use estimation to help you divide correctly.

a.  $\begin{array}{r} 21 \text{ r.3} \\ 16 \overline{)339} \\ \underline{-32} \phantom{0} \\ 19 \\ \underline{-16} \\ 3 \end{array}$       b.  $\begin{array}{r} 56 \text{ r.12} \\ 15 \overline{)832} \\ \underline{-75} \phantom{0} \\ 102 \\ \underline{-90} \\ 12 \end{array}$       c.  $\begin{array}{r} 17 \text{ r.1} \\ 22 \overline{)375} \\ \underline{-22} \phantom{0} \\ 155 \\ \underline{-154} \\ 1 \end{array}$

2. Find each quotient. A list of multiples is provided to help you divide correctly.

a.  $\begin{array}{r} 28 \text{ r.7} \\ 24 \overline{)679} \\ \underline{-48} \phantom{0} \\ 199 \\ \underline{-192} \\ 7 \end{array}$       b.  $\begin{array}{r} 431 \text{ r.11} \\ 13 \overline{)5614} \\ \underline{-52} \phantom{0} \\ 41 \\ \underline{-39} \\ 24 \\ \underline{-24} \\ 0 \end{array}$

$24 \times 1 = 24$        $13 \times 1 = 13$   
 $24 \times 2 = 48$        $13 \times 2 = 26$   
 $24 \times 3 = 72$        $13 \times 3 = 39$   
 $24 \times 4 = 96$        $13 \times 4 = 52$   
                           $13 \times 5 = 65$   
                           $13 \times 6 = 78$   
                           $13 \times 7 = 91$

3. Find each quotient. First, write out a list of the multiples on a separate sheet of paper and then divide.

a.  $\begin{array}{r} 31 \text{ r.2} \\ 15 \overline{)487} \\ \underline{-45} \phantom{0} \\ 37 \\ \underline{-35} \\ 2 \end{array}$       b.  $\begin{array}{r} 39 \text{ r.17} \\ 22 \overline{)875} \\ \underline{-66} \phantom{0} \\ 215 \\ \underline{-198} \\ 17 \end{array}$

## LESSON 7

It is very common for students to mix up exponents with multiplication. For instance, a student might mistakenly write  $2^3 = 6$ . The best way to combat that is to keep having students write out what the exponent represents,  $2^3 = 2 \times 2 \times 2$ , until it really clicks.

### Page 37 Answers

EXPONENTS LESSON 7

**ACTIVITY**

**EXPONENTS**

**Exponent Exploration**

You Will Need:

- Beans (or another small counter to act out the problem)
- Calculator

You Will Do:

1. Brandon's grandmother offers him two options for his Christmas present. In option 1, he can choose to receive \$36. In option 2, he can receive \$2 on the first day, \$4 on the second day, and \$8 on the third day, with the amount doubling each day for 10 days. Which option would you choose?

2. Act out the problem with your beans or another counter. Let each bean represent \$1. Write in the amount of money that Brandon would receive each day if he chooses option 2.

Day 1	Day 2	Day 3	Day 4	Day 5	Day 6	Day 7	Day 8	Day 9	Day 10
\$2	\$4	\$8	16	32	64	128	256	512	1,024

3. Use your calculator to add up the total amount.

Total for Option 1: 36

Total for Option 2: 2,046

You have already learned that you can use multiplication instead of doing repeated addition.

$3 + 3 + 3 + 3 + 3 = 15$  or  $3 \times 5 = 15$

37

### Page 39 Answers

EXPONENTS LESSON 7

1. Write the expression using exponents.

- $3 \times 3 \times 3 = 3^3$
- $6 \times 6 \times 6 \times 6 = 6^4$
- $8 \times 8 \times 8 \times 8 \times 8 = 8^5$
- $10 \times 10 = 10^2$
- $5 \times 5 \times 5 \times 6 \times 6 = 5^3 \times 6^2$

2. Write out the expression using repeated multiplication.

- $7^3 = 7 \times 7 \times 7$
- $2^3 = 2 \times 2 \times 2$
- $5^5 = 5 \times 5 \times 5 \times 5 \times 5$
- $4^7 \times 2^6 = 4 \times 4 \times 4 \times 4 \times 2 \times 2 \times 2 \times 2 \times 2$

3. Use your calculator to find the missing exponent for each equation.

- $2^5 = 32$
- $6^{23} = 1,296$
- $3^5 = 243$
- $4^{23} = 256$

39

## LESSON 8

I love teaching this concept visually with squares and the sides of squares. It is also really important to emphasize the inverse relationship between the two operations. Inverse operations are a key overarching concept in mathematics and will become essential when students start solving equations.

### Page 42 Answers

LESSON 8 SQUARES AND SQUARE ROOTS

The square root of 81 is 9, because if we square 9 (multiplying 9 by itself) we will get 81.

**EXAMPLE 2: Find the square root of each number.**

$\sqrt{4} = 2$ ,  $\sqrt{49} = 7$ ,  $\sqrt{64} = 8$

We need to think of what number we can square to get each of the results that are under the square root sign.

$\sqrt{4} = 2$ ,  $\sqrt{49} = 7$ ,  $\sqrt{64} = 8$

1. Square each of the numbers below.

- $8^2 = 64$
- $11^2 = 121$
- $6^2 = 36$
- $13^2 = 169$

2. Find each square root.

- $\sqrt{9} = 3$
- $\sqrt{1} = 1$
- $\sqrt{81} = 9$
- $\sqrt{25} = 5$
- $\sqrt{100} = 10$
- $\sqrt{169} = 13$
- $\sqrt{4} = 2$
- $\sqrt{16} = 4$

42

### Page 43 Answers

SQUARES AND SQUARE ROOTS LESSON 8

3. A square tile has a side length of 9 inches. What is the area of the tile in square inches?

81 square inches

4. The area of a square garden is 25 square feet. What is the length of one side of the garden?

5 feet

5. A square blanket has an area of 36 square feet. What is the length of one side of the blanket?

6 feet

**CHALLENGE!**

Two square numbers have a sum of 25. What are the two numbers?

9 + 16

43

## LESSON 9

Some students think of Please Excuse My Dear Aunt Sally to remember the acronym PEMDAS.

One of the most common mistakes when solving order of operations problems is to not realize that you do addition and subtraction together from left to right. The same goes for multiplication and division. If there is a division sign to the left of a multiplication sign, that is what you do first.

$$10 \div 5 \times 3 =$$

$$2 \times 3 =$$

$$6$$

### Page 46 Answers

**LESSON 9 THE ORDER OF OPERATIONS (DAY ONE)**

Evaluate each expression. Remember to use PEMDAS through each stage of solving. Look at your foldable if you need help remembering the steps.

a. $5 + 21 - 3 \times 2$ $5 + 7 \times 2$ $5 + 14$ $19$	b. $9 + (82 - 12)$ $9 + 50$ $59$
c. $33 + (15 - 4) + 3$ $33 \div 11 + 3$ $3 + 3$ $6$	d. $(7 + 42) - 2 \times 3$ $49 - 2 \times 3$ $49 - 6$ $43$
e. $16 + 12 + 4 - 2^3$ $16 + 12 \div 4 - 4$ $16 + 3 - 4$ $19 - 4$ $15$	f. $81 \div 3^2$ $81 \div 9$ $9$
g. $10^2 - 60 \div 6$ $100 - 60 \div 6$ $100 - 10$ $90$	h. $4 \times 5^2 + (3 + 2)$ $4 \times 5^2 + 5$ $4 \times 25 + 5$ $100 + 5$ $105$

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## LESSON 10

Another day of practice with the order of operations. Most students will need this second day to really grasp the steps.

### Page 47 Answers

**THE ORDER OF OPERATIONS (DAY TWO) LESSON 10**

**WARM UP**  
The first letter of each step in the order of operations is written below. Do your best to write in the name of each step. Then, use your foldable from the last lesson to fill in any steps you forgot.

P Parenttheses  
E Exponents  
M/D Multiplication / Division  
A/S Addition / Subtraction

1. Evaluate each expression. Use your foldable to help you remember the steps.

a. $5 \times (5 + 1) - 7$ $5 \times 6 - 7$ $30 - 7$ $23$	b. $(8 + 2)^2 + 3 + 8$ $(8 + 4) \div 3 + 9$ $12 \div 3 + 9$ $4 + 9$ $13$
c. $4 \times 3 + (8 - 9) + 3^2$ $12 + (0) + 9$ $12 + 9$ $21$	d. $20 + 10 \div 2 - 3^2$ $20 + 10 \div 2 - 9$ $20 + 5 - 9$ $25 - 9$ $16$
e. $21 + (15 - 8) + 30$ $21 \div 7 + 10$ $3 + 10$ $13$	f. $64 \div (2^2 + 4)$ $64 \div (4 + 4)$ $64 \div 8$ $8$

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# CHAPTER 2: MULTIPLICATION, FACTORS, AND MULTIPLES

## LESSON 12

They play the game in this lesson using tenths. They will play it again in the next lesson with subtraction and in Lesson 13 with hundredths.

### Page 54 Answers

**LESSON 12** ADDING DECIMALS

1. Find each sum.

a.  $1.4 + 2.8 = 4.2$

b.  $3.45 + 4.08 = 7.53$

c.  $0.98 + 1.20 = 2.18$

d.  $3.200 + 1.089 = 4.289$

2. Rewrite each problem vertically, being careful to line up the decimal points. Then find the sum.

a.  $1.7 + 2.1 = 3.8$

b.  $3.047 + 21.2 = 24.247$

c.  $3.43 + 1.90 = 5.33$

d.  $20.11 + 13.27 = 33.38$

54

### Page 55 Answers

**LESSON 12** ADDING DECIMALS

a.  $3.43 + 1.9 = 5.33$

b.  $6.54 + 1.3 = 7.84$

c.  $7.787 + 0.4 = 8.187$

d.  $8.17 + 10.87 = 19.04$

e.  $5 + 1.83 = 6.83$

f.  $6.84 + 1.97 = 8.81$

3. Winona spent \$10.59 at the store, and Ruby spent \$13.78. How much did they spend altogether?

$10.59 + 13.78 = 24.37$

\$24.37

55

## LESSON 13

Now students are subtracting and moving backward on the gameboard.

### Page 57 Answers

**LESSON 13** SUBTRACTING DECIMALS

**EXAMPLE 2:** Find the difference.  $33.25 - 1.43 =$

Line up the problem vertically, making sure the decimal points line up.

$33.25 - 1.43 = 31.82$

**EXAMPLE 3:** Isiah buys a toy that costs \$17.83. He pays the cashier \$20. How much change should he receive back?

We need to subtract the cost of the toy from the amount he gave the cashier.

$20.00 - 17.83 = 2.17$

He should receive \$2.17 in change.

1. Find each difference.

a.  $3.9 - 1.7 = 2.2$

b.  $1.75 - 1.03 = 0.72$

c.  $3.15 - 1.98 = 1.17$

d.  $7.4 - 1.9 = 5.5$

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Page 58 Answers

LESSON 13 SUBTRACTING DECIMALS

2. Rewrite each problem vertically, being careful to line up the decimal points. Then find the difference.

a.  $2.5 - 1.1$

$$\begin{array}{r} 2.5 \\ - 1.1 \\ \hline 1.4 \end{array}$$

b.  $20.99 - 2.34$

$$\begin{array}{r} 20.99 \\ - 2.34 \\ \hline 18.65 \end{array}$$

c.  $20.9 - 1.85$

$$\begin{array}{r} 20.90 \\ - 1.85 \\ \hline 19.25 \end{array}$$

d.  $19.09 - 1.7$

$$\begin{array}{r} 19.09 \\ - 1.70 \\ \hline 17.39 \end{array}$$

e.  $3.43 - 0.907$

$$\begin{array}{r} 3.430 \\ - 0.907 \\ \hline 2.523 \end{array}$$

f.  $10.3 - 1.77$

$$\begin{array}{r} 10.30 \\ - 1.77 \\ \hline 8.53 \end{array}$$

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Page 59 Answers

LESSON 13 SUBTRACTING DECIMALS

a.  $20.11 - 13.27$

$$\begin{array}{r} 20.11 \\ - 13.27 \\ \hline 6.84 \end{array}$$

b.  $7.787 - 3.43$

$$\begin{array}{r} 7.787 \\ - 3.430 \\ \hline 4.357 \end{array}$$

c.  $16.313 - 1.92$

$$\begin{array}{r} 16.313 \\ - 1.920 \\ \hline 14.393 \end{array}$$

d.  $116.65 - 70.89$

$$\begin{array}{r} 116.65 \\ - 70.89 \\ \hline 45.76 \end{array}$$

3. Simon is purchasing apples that cost \$13.56. He pays with \$15. How much change should he receive?

$$\begin{array}{r} 15.00 \\ - 13.56 \\ \hline 1.44 \end{array}$$

59

LESSON 14

Adding hundredths repeatedly can quickly become complicated. That is why I have them round the answers. It also allows them to use the same gameboard. Rounding is a skill that students struggle with consistently, so it is good for them to have some practice with it in this game.

Page 62 Answers

LESSON 14 ADDING AND SUBTRACTING DECIMALS

Use your knowledge of decimals to solve each word problem.

1. Sylvia is making hair bows to sell at a craft show. She already has three lengths of ribbon in her craft bin that she plans to use. The ribbons are 37.1 inches, 26.45 inches, and 10.5 inches long. How many total inches of ribbon does she have?

$$\begin{array}{r} 37.10 \\ + 26.45 \\ + 10.50 \\ \hline 74.05 \end{array}$$

74.05 inches of ribbon

2. She bought metal clasps for \$5.49 and a hot glue gun for \$15.25. How much did she spend total on the clasps and the hot glue gun?

$$\begin{array}{r} 15.25 \\ + 5.49 \\ \hline 20.74 \end{array}$$

\$20.74

3. She had \$30 set aside to buy supplies. How much money does she have left after buying the clasps and hot glue gun?

$$\begin{array}{r} 30.00 \\ - 20.74 \\ \hline 9.26 \end{array}$$

\$9.26

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Page 63 Answers

LESSON 14 ADDING AND SUBTRACTING DECIMALS

4. She has a length of elastic that is 12.5 inches long. She cuts off a piece that is 3.25 inches long to make a small scrunchie. How much elastic is left?

$$\begin{array}{r} 12.50 \\ - 3.25 \\ \hline 9.25 \end{array}$$

9.25 inches

5. In the first hour of the craft show, she sells three items. The items cost \$5.75, \$6.71, and \$3.28. How much money did she make total in the first hour?

$$\begin{array}{r} 5.75 \\ + 6.71 \\ + 3.28 \\ \hline 15.74 \end{array}$$

\$15.74

6. If she wants to make twice as much in the second hour, how many dollars' worth of hair bows does she need to sell in the second hour?

$$\begin{array}{r} 15.74 \\ + 15.74 \\ \hline 31.48 \end{array}$$

\$31.48

63



## LESSON 17

In addition to teaching a new skill, this lesson is also a great review of the long division process.

### Page 71 Answers

DIVIDING DECIMALS LESSON 17

**ACTIVITY**

### LESSON 17: DIVIDING DECIMALS

#### Dividing Grids

**You Will Need:**

- Lesson 17 Activity Sheet
- Scissors

**You Will Do:**

- Carefully tear out the activity sheet from the back of the answer key. Color in the grids to show the decimal 1.17. Cut out the divided grids of your grid.
- Now we are going to model the problem below. Cut apart the grid for number 1.17, and split it into 9 even piles.

1.17 = 0.13

- Find the quotient by counting the answer in each pile.

When we divide a decimal by a whole number, we can follow the same steps for long division. **The only difference** is that we need to pay attention to one thing. We need to pay attention to the decimal point and write it in the correct place in our quotient. And we need to make sure there are no decimals in the divisor.

**Steps for Long Division With Decimals**

- Write the decimal point in the correct spot above the dividend.
- Divide into the first place value that you can divide without regrouping. Write the quotient above.
- Multiply the quotient by the divisor to check and see how many hundreds, tens or ones you used.
- Subtract to find out if there are any remainders.
- Bring down. Repeat steps 1-3 until the whole number has been divided.

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### Page 74 Answers

LESSON 17 DIVIDING DECIMALS

**ACTIVITY**

### LESSON 17: DIVIDING DECIMALS

**1. Find each quotient.**

a. 
$$\begin{array}{r} 8.1 \\ 4 \overline{)32.4} \\ \underline{-32} \phantom{0} \\ 04 \\ \underline{-4} \\ 0 \end{array}$$

b. 
$$\begin{array}{r} 31.67 \\ 3 \overline{)95.01} \\ \underline{-93} \phantom{00} \\ 20 \\ \underline{-18} \\ 21 \\ \underline{-21} \\ 0 \end{array}$$

c. 
$$\begin{array}{r} 4.18 \\ 2 \overline{)8.36} \\ \underline{-8} \phantom{00} \\ 03 \\ \underline{-2} \\ 16 \\ \underline{-16} \\ 0 \end{array}$$

**2. Find each quotient. First, multiply the divisor and dividend so that there are no decimals. Sometimes you will need to multiply by 10 and sometimes by 100. The first two problems are started for you.**

a. 
$$\begin{array}{r} 1.6 \overline{)24.8} \\ \underline{16} \phantom{00} \\ 88 \\ \underline{-80} \\ 80 \\ \underline{-80} \\ 0 \end{array}$$

b. 
$$\begin{array}{r} 0.56 \overline{)28} \\ \underline{56} \phantom{00} \\ 56 \\ \underline{-56} \\ 0 \end{array}$$

c. 
$$\begin{array}{r} 0.9 \overline{)81} \\ \underline{90} \\ -81 \\ \underline{00} \\ -0 \\ 0 \end{array}$$

d. 
$$\begin{array}{r} 0.03 \overline{)10.47} \\ \underline{30} \phantom{00} \\ 1047 \\ \underline{-900} \\ 147 \\ \underline{-120} \\ 27 \\ \underline{-27} \\ 0 \end{array}$$

e. 
$$\begin{array}{r} 0.7 \overline{)21} \\ \underline{70} \\ -21 \\ \underline{00} \\ -0 \\ 0 \end{array}$$

f. 
$$\begin{array}{r} 0.2 \overline{)3.6} \\ \underline{20} \\ -2 \\ \underline{10} \\ -10 \\ 0 \end{array}$$

**3. Sarah has \$3.92. How many \$0.49 stamps can she buy?**

$$\begin{array}{r} 8 \\ 49 \overline{)392} \\ \underline{-343} \\ 49 \end{array}$$

8 stamps

74

## LESSON 18

We definitely need a review lesson after all of those decimal skills. And why not teach some money management at the same time? That was a bonus for all of you parents. Additionally, kids are far more motivated to do math when given a context like the one in this lesson.

### Page 75 Answers

DECIMAL MIXED REVIEW LESSON 18

**ACTIVITY**

### LESSON 18: DECIMAL MIXED REVIEW

#### Takeout Night Money Management

**You Will Need:**

- A takeout menu from a restaurant with prices listed (you can tear out the sample menu from the back of the answer key)
- A calculator

**You Will Do:**

[Sample Answer](#)

1. First, we will use the takeout menu and your decimal math skills to plan a takeout lunch for yourself. You have \$20 to spend. Begin by choosing 2-3 items off the menu that you would like to order. Make a meal and a drink! It is up to you. Just make sure the total is not over \$20. List the items below.

Item #1: Veggie Samosa Cost: 5 20

Item #2: Chicken Biryani Cost: 14 55

Item #3: \_\_\_\_\_ Cost: \_\_\_\_\_

2. Add up the costs of the items you ordered to find the total. Check your answer with a calculator.

$$\begin{array}{r} 14.55 \\ + 5.20 \\ \hline 19.75 \end{array}$$

3. Suppose you pay for your lunch with a \$20 bill. How much change should you receive back?

$$\begin{array}{r} 20.00 \\ - 19.75 \\ \hline 0.25 \end{array}$$

75

Page 76 Answers

LESSON 18 DECIMAL MIXED REVIEW

4. Now let's plan a meal for some family and friends. You can decide who you want to invite. You have room for up to 7 people. Write the names below.

Sara
Katy
Andrea
Elysia
Total Number of people = <u>4</u>

5. Choose an appetizer from the restaurant menu. You are going to order 3 orders of the appetizer to make sure everyone gets to have plenty. Multiply the price by 3 to find the total. Check your answer on your calculator.

Appetizer: Papri chaat Price: 6 23

$$\begin{array}{r} 6.23 \\ \times 3 \\ \hline 18.69 \end{array}$$

**\$18.69**

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Page 77 Answers

DECIMAL MIXED REVIEW LESSON 18

6. Now select a meal for each of your guests and don't forget to add one for yourself! Find the total. You can use your calculator for this depending on how many guests you invited.

$$\begin{array}{r} 15.59 \\ 14.55 \\ 14.55 \\ 12.47 \\ + 17.67 \\ \hline 74.83 \end{array}$$

7. Add the cost of the appetizers to the total for the meals.

$$\begin{array}{r} 74.83 \\ + 18.69 \\ \hline 93.52 \end{array}$$

8. Suppose you want to calculate how much you spent on average on each of your guests. Divide the total cost by the number of guests you invited. You can round your answer to the nearest hundredth or penny.

$$\begin{array}{r} 18.70 \\ 5 \overline{)93.52} \\ \underline{-5} \phantom{00} \\ 43 \phantom{00} \\ \underline{-40} \phantom{00} \\ 35 \phantom{00} \\ \underline{-35} \phantom{00} \\ 02 \phantom{00} \\ \underline{-0} \phantom{00} \\ 2 \phantom{00} \\ \underline{-2} \phantom{00} \\ 0 \phantom{00} \end{array}$$

The average you spent is 18.70 per guest.

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LESSON 19

In each unit there will be one problem-solving lesson. There is a complete description of this program element in the beginning of this book. The main thing to keep in mind is that the process is more important than the results. Your child can be making a lot of progress but still not find the right answer.

Page 81 Answers

PROBLEM SOLVING PRACTICE #1 LESSON 19

Solve each problem below using any strategy you like. Once you check your answer, explain what you did to your parent.

Sample Answer

1. Mia makes a list of the even numbers from 0 to 50. How many times does 2 appear as a digit on her list?

0 (2) 4 6 8 10 (2) 16 18 (20)  
 (22) (24) (26) (28) 30 (32) 34 36  
 38 40 (42) 44 46 48 50

10 times

2. In the puzzle below, each letter stands for a different digit. Neither number is zero. Can you find the value of each letter?

A is 5  
 B is 1

$$\begin{array}{r} A \quad 5 \\ A \quad 5 \\ + A \quad +5 \\ \hline BA \quad 15 \end{array}$$

81



## LESSON 21

The two main repeating decimals to memorize are  $1/3 = 0.3333\dots$  and  $2/3 = 0.6666\dots$ . Because of this, there are two new cards included to be added to the game from Lesson 20.

The four operations needed on your calculator are addition, subtraction, multiplication, and division. Any simple and inexpensive calculator will have these.

### Page 88 Answers

**LESSON 21: REPEATING DECIMALS**  
Calculator Conversions

**You Will Need:**

- A four-operation calculator
- Lesson 21: Activity Sheet (to be used later)

**You Will Do:**

- Use our answer between a fraction and a decimal on a calculator. It is a helpful way to check your answers. Convert each of these fractions to decimals by dividing the numerator by the denominator on your calculator.
  - $\frac{3}{4} = 0.75$
  - $\frac{1}{2} = 0.6$
  - $\frac{7}{10} = 0.7$
  - $\frac{29}{106} = 0.29$
- Not every fraction can be converted easily to a decimal. Try converting the decimals below. Tell your partner what happens.
  - $\frac{1}{3} = 0.33\dots$
  - $\frac{2}{11} = 0.3636\dots$  The digits repeat.

### Page 91 Answers

**LESSON 21**

- Rewrite each repeating decimal below using the bar notation. The first one is done for you.
  - $0.06060606\dots = 0.\overline{06}$
  - $0.8181818181\dots = 0.\overline{81}$
  - $0.44444444\dots = 0.\overline{4}$
  - $22.33333333\dots = 22.\overline{3}$
  - $0.3535353535\dots = 0.\overline{35}$
- The fractions below convert to repeating decimals. Use your calculator to convert them. Write just the tenths and hundredths digits in the space provided. Then write 3 dots to the right to show that the decimal repeats.
  - $\frac{2}{3} = 0.\underline{\quad}66\dots$
  - $\frac{3}{11} = 0.\underline{\quad}27\dots$
  - $\frac{2}{9} = 0.\underline{\quad}22\dots$
  - $\frac{5}{11} = 0.\underline{\quad}45\dots$

### Page 92 Answers

**LESSON 21**

- Use your calculator to convert these fractions to decimals. If the decimal is a repeating decimal, use the bar notation to write it.
  - $\frac{4}{5} = 0.8$
  - $\frac{33}{100} = 0.33$
  - $\frac{2}{3} = 0.\overline{6}$
  - $\frac{2}{9} = 0.\overline{2}$
  - $\frac{3}{10} = 0.3$
  - $\frac{5}{8} = 0.625$
  - $\frac{1}{60} = 0.\overline{3}$
  - $\frac{3}{11} = 0.\overline{27}$
  - $\frac{4}{9} = 0.\overline{4}$
  - $\frac{9}{20} = 0.45$
- Use long division to convert the two fractions below to decimals.
  - $\frac{3}{25} = 0.12$
  - $\frac{8}{9} = 0.88\dots$

$$\begin{array}{r} 25 \overline{) 3.00} \\ \underline{- 25} \phantom{0} \\ 50 \\ \underline{- 50} \\ 0 \end{array}$$

$$\begin{array}{r} 9 \overline{) 8.0} \\ \underline{- 72} \\ 80 \\ \underline{- 72} \\ 8 \end{array}$$
- Use the Lesson 21 activity sheet from the back of the answer key. Cut out the additional cards. Mix them in with the cards from Lesson 20, and play one round of memory with the new cards included.

## LESSON 22

To add and subtract fractions, you essentially “unsimplify” them so that you can perform the operation. Because of this, you often must simplify again at the end when you have your answer.

### Page 93 Answers

ADDING AND SUBTRACTING FRACTIONS LESSON 22

**WARM UP**  
Rewrite each pair of fractions with a common denominator.

a.  $\frac{15}{18} + \frac{4}{18}$     b.  $\frac{8}{56} + \frac{21}{56}$

c.  $\frac{4}{6} + \frac{1}{6}$     d.  $\frac{7}{14} + \frac{8}{14}$

In this lesson, we will review how to add and subtract fractions.

**Steps for Adding and Subtracting Fractions**

1. If the fractions have unlike denominators, rewrite them with common denominators.
2. Add or subtract.
3. Simplify your answer.

**EXAMPLE 1:** Find the sum,  $\frac{2}{3} + \frac{3}{12} =$

$\frac{2 \times 4}{3 \times 4} = \frac{8}{12}$     The fractions have different denominators. We will need to rewrite them with a common denominator. The least common denominator is 12.

$\frac{8}{12} + \frac{3}{12} =$     Now we can add.

$\frac{8}{12} + \frac{3}{12} = \frac{11}{12}$     Simplify the answer.

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### Page 95 Answers

ADDING AND SUBTRACTING FRACTIONS LESSON 22

Find each sum or difference. Use the answers to crack the code below.

O	$\frac{5}{6} + \frac{1}{6} =$ $\frac{5}{6} + \frac{1}{6} =$ $\frac{6}{6} = 1$	S	$\frac{5}{12} + \frac{7}{12} =$ $\frac{5}{12} + \frac{7}{12} =$ $\frac{12}{12} = 1$	T	$\frac{5}{12} - \frac{1}{12} =$ $\frac{5}{12} - \frac{1}{12} =$ $\frac{4}{12} = \frac{1}{3}$
O	$\frac{1}{15} + \frac{1}{15} =$ $\frac{1}{15} + \frac{1}{15} =$ $\frac{2}{15}$	P	$\frac{4}{15} + \frac{1}{3} =$ $\frac{4}{15} + \frac{5}{15} =$ $\frac{9}{15} = \frac{3}{5}$	F	$\frac{11}{12} + \frac{1}{12} =$ $\frac{11}{12} + \frac{1}{12} =$ $\frac{12}{12} = 1$
E	$\frac{7}{16} + \frac{1}{4} =$ $\frac{7}{16} + \frac{4}{16} =$ $\frac{11}{16}$	T	$\frac{7}{8} - \frac{3}{8} =$ $\frac{7}{8} - \frac{3}{8} =$ $\frac{4}{8} = \frac{1}{2}$	S	$\frac{6}{11} - \frac{1}{11} =$ $\frac{6}{11} - \frac{1}{11} =$ $\frac{5}{11}$

**THE MORE YOU TAKE, THE MORE YOU LEAVE BEHIND. WHAT AM I?**

**F O O T S T E P S**

$\frac{11}{12} + \frac{1}{15} = \frac{25}{20}$      $\frac{5}{6} = \frac{10}{12}$      $\frac{5}{12} + \frac{1}{12} = \frac{6}{12} = \frac{1}{2}$      $\frac{1}{8} = \frac{1.5}{12}$      $\frac{11}{18} = \frac{22}{36}$      $\frac{2}{3} = \frac{16}{24}$      $\frac{7}{33} = \frac{14}{66}$

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## LESSON 23

Bear with your student in this lesson. There are many layered skills when you add and subtract mixed numbers. There is regrouping in addition to all the skills they just practiced in Lesson 22.

### Page 99 Answers

ADD AND SUBTRACT MIXED NUMBERS (DAY ONE) LESSON 23

1. Rewrite each improper fraction as a mixed number.

a.  $\frac{7}{2} = \frac{4}{2} + \frac{3}{2} = 2\frac{3}{2}$     b.  $\frac{7}{6} = \frac{6}{6} + \frac{1}{6} = 1\frac{1}{6}$

c.  $\frac{21}{20} = \frac{20}{20} + \frac{1}{20} = 1\frac{1}{20}$     d.  $\frac{8}{5} = \frac{5}{5} + \frac{3}{5} = 1\frac{3}{5}$

2. Rewrite each mixed number as an improper fraction.

a.  $1\frac{3}{2} = \frac{5}{2}$     b.  $3\frac{1}{3} = \frac{10}{3}$

c.  $4\frac{3}{7} = \frac{30}{7}$     d.  $1\frac{3}{4} = \frac{7}{4}$

3. Find each sum or difference.

a.	$\begin{array}{r} 1\frac{1}{3} \\ + 3\frac{1}{3} \\ \hline 4\frac{2}{3} \end{array}$	b.	$\begin{array}{r} 2\frac{2}{5} \\ - 1\frac{1}{5} \\ \hline 1\frac{1}{5} \end{array}$
----	--	----	--

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### Page 100 Answers

LESSON 23 ADD AND SUBTRACT MIXED NUMBERS (DAY ONE)

a.	$\begin{array}{r} 3\frac{5}{10} \\ + 3\frac{4}{10} \\ \hline 6\frac{9}{10} \end{array}$	b.	$\begin{array}{r} 1\frac{5}{12} \\ + 3\frac{3}{12} \\ \hline 4\frac{8}{12} = 4\frac{2}{3} \end{array}$
c.	$\begin{array}{r} 2\frac{9}{10} \\ - 1\frac{4}{10} \\ \hline 2\frac{5}{10} = 2\frac{1}{2} \end{array}$	d.	$\begin{array}{r} 4\frac{4}{6} \\ - 1\frac{3}{6} \\ \hline 3\frac{1}{6} \end{array}$
e.	$\begin{array}{r} 2\frac{1}{5} \\ + 1\frac{15}{20} \\ \hline 3\frac{19}{20} \end{array}$	f.	$\begin{array}{r} 1\frac{5}{15} \\ + 1\frac{9}{15} \\ \hline 2\frac{14}{15} \end{array}$

4. Mary has used  $5\frac{1}{4}$  total cups of flour in a bread recipe. Some of it was whole wheat and the rest was white flour. If she knows she used  $2\frac{1}{4}$  cups of whole wheat flour, how much white flour did she use?

$3\frac{1}{4}$  cups     $5\frac{1}{4} - 2\frac{1}{4} = 3\frac{0}{4} = 3$      $5\frac{2}{4} - 2\frac{1}{4} = 3\frac{1}{4}$

100

## LESSON 24

I added a second day of mixed numbers because most students will need it. And this concept has built in review of regrouping and simplifying fractions.

### Page 101 Answers

ADD AND SUBTRACT MIXED NUMBERS (DAY TWO) LESSON 24

**WARM UP**  
Rewrite each improper fraction as a mixed number.

a.  $\frac{7}{3} = \frac{6}{3} + \frac{1}{3} = 2\frac{1}{3}$       b.  $\frac{10}{7} = \frac{7}{7} + \frac{3}{7} = 1\frac{3}{7}$

c.  $\frac{9}{5} = \frac{5}{5} + \frac{4}{5} = 1\frac{4}{5}$       d.  $\frac{11}{10} = \frac{10}{10} + \frac{1}{10} = 1\frac{1}{10}$

Rewrite each mixed number as an improper fraction.

a.  $3\frac{1}{2} = \frac{7}{2}$       b.  $4\frac{1}{7} = \frac{29}{7}$

c.  $2\frac{3}{8} = \frac{19}{8}$       d.  $5\frac{1}{3} = \frac{16}{3}$

Sometimes when we are adding mixed numbers, we will need to regroup.

**EXAMPLE 1:** Find the difference.  $2\frac{3}{8} - 1\frac{5}{8}$

Line up the mixed numbers vertically. Then rewrite the fractions with a common denominator.

$2\frac{3}{8}$	$2\frac{9}{24}$
$- 1\frac{5}{8}$	$- 1\frac{10}{24}$
$\hline$	$\hline$

We cannot subtract  $\frac{10}{24}$  from  $\frac{9}{24}$ . We will need to regroup first.

$$2\frac{9}{24} = 1 + \frac{24}{24} + \frac{9}{24} = 1\frac{33}{24}$$

101

### Page 103 Answers

ADD AND SUBTRACT MIXED NUMBERS (DAY TWO) LESSON 24

Find each sum or difference.

a.

$4\frac{2}{5}$	$4\frac{4}{10}$
$- 1\frac{1}{10}$	$- 1\frac{1}{10}$
$\hline$	$\hline$

b.

$3\frac{1}{3}$	$3\frac{2}{9}$
$+ 1\frac{1}{9}$	$+ 1\frac{1}{9}$
$\hline$	$\hline$

c.

$2\frac{1}{10}$	$2\frac{1}{10}$	$1\frac{11}{10}$
$- 1\frac{3}{10}$	$- 1\frac{4}{10}$	$- 1\frac{4}{10}$
$\hline$	$\hline$	$\hline$

d.

$3\frac{3}{15}$	$3\frac{9}{15}$
$+ 1\frac{10}{15}$	$+ 1\frac{10}{15}$
$\hline$	$\hline$

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### Page 104 Answers

LESSON 24 ADD AND SUBTRACT MIXED NUMBERS (DAY TWO)

a.

$3\frac{3}{12}$	$3\frac{4}{12}$	$2\frac{16}{12}$
$- 1\frac{7}{12}$	$- 1\frac{6}{12}$	$- 1\frac{6}{12}$
$\hline$	$\hline$	$\hline$

b.

$1\frac{3}{10}$	$1\frac{15}{20}$
$+ 1\frac{9}{10}$	$+ 1\frac{6}{20}$
$\hline$	$\hline$

c.

$3\frac{3}{9}$	$3\frac{6}{9}$
$+ 1\frac{4}{9}$	$+ 1\frac{4}{9}$
$\hline$	$\hline$

d.

$3\frac{3}{10}$	$3\frac{3}{10}$	$2\frac{13}{10}$
$- 1\frac{7}{10}$	$- 1\frac{4}{10}$	$- 1\frac{4}{10}$
$\hline$	$\hline$	$\hline$

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## LESSON 25

While it is harder to grasp conceptually, multiplying fractions is a much easier operation to execute. This lesson will probably feel much more manageable than what we have been working on earlier in the chapter. This lesson is also laying the groundwork for the skills students will need when converting units in future science classes.

### Page 105 Answers

MULTIPLY FRACTIONS LESSON 25

**ACTIVITY**

**LESSON 25: MULTIPLY FRACTIONS**

**Fill the Squares**

**You Will Need:**

- Lesson 25 Activity Sheet
- 2 different colored counters (this can be straws or small game pieces)

**You Will Do:**

- We are going to use the counters to act out fraction multiplication. Tear out the activity sheet from the back of the answer key. Start with the grid that has 12 squares. Using vertical columns, cover  $\frac{2}{3}$  of the squares with the first kind of counter.
- Using horizontal rows, cover  $\frac{1}{3}$  of the squares with the second kind of counter.
- How many squares have both kinds of counters in them? Can you simplify this fraction?
 
$$\frac{2}{12} = \frac{1}{6}$$
- Use the 12-grid to act out these fraction problems. Always do the first fraction with vertical columns and the second fraction with horizontal rows.
 
$$\frac{1}{3} \times \frac{2}{3} = \frac{2}{9}$$

$$\frac{1}{4} \times \frac{3}{4} = \frac{3}{16}$$

$$\frac{1}{5} \times \frac{2}{5} = \frac{2}{25}$$

$$\frac{1}{6} \times \frac{3}{6} = \frac{3}{36}$$

$$\frac{1}{8} \times \frac{3}{8} = \frac{3}{64}$$

$$\frac{1}{9} \times \frac{2}{9} = \frac{2}{81}$$

$$\frac{1}{10} \times \frac{3}{10} = \frac{3}{100}$$

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### Page 106 Answers

LESSON 25 MULTIPLY FRACTIONS

5. Use the 24-grid to act out these fraction problems. Always do the first fraction with vertical columns and the second fraction with horizontal rows.

$$\frac{1}{3} \times \frac{2}{3} = \frac{2}{9}$$

$$\frac{1}{4} \times \frac{3}{4} = \frac{3}{16}$$

$$\frac{1}{5} \times \frac{2}{5} = \frac{2}{25}$$

$$\frac{1}{6} \times \frac{3}{6} = \frac{3}{36}$$

$$\frac{1}{8} \times \frac{3}{8} = \frac{3}{64}$$

$$\frac{1}{9} \times \frac{2}{9} = \frac{2}{81}$$

$$\frac{1}{10} \times \frac{3}{10} = \frac{3}{100}$$

6. Why do you think you need to switch from the 12-grid to the 24-grid to act out the second set of problems?

Answers will vary.

When we multiply fractions, we just need to multiply the numerators by the numerators and the denominators by the denominators. Many students find multiplying easier than adding and subtracting. The biggest pit can be simplifying at the end. Because of this, it is often a good idea to divide out any common factors before multiplying.

$$\frac{2}{3} \times \frac{1}{3} = \frac{2}{9}$$

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### Page 109 Answers

MULTIPLY FRACTIONS LESSON 25

1. Find each product. Be sure to simplify your answer.

- $\frac{1}{3} \times \frac{5}{6} = \frac{5}{24}$
- $\frac{1}{5} \times \frac{5}{3} = \frac{1}{3}$
- $\frac{1}{7} \times \frac{1}{7} = \frac{1}{49}$
- $\frac{5}{6} \times \frac{5}{6} = \frac{25}{36}$
- $\frac{1}{1} \times \frac{1}{4} = \frac{1}{4}$
- $\frac{1}{3} \times \frac{1}{3} = \frac{1}{9}$
- $\frac{1}{1} \times \frac{1}{4} = \frac{1}{4}$
- $\frac{3}{10} \times \frac{1}{2} = \frac{3}{20}$

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### Page 110 Answers

LESSON 25 MULTIPLY FRACTIONS

- $6 \times \frac{1}{3} = 2$
- $\frac{2}{1} \times \frac{1}{3} = \frac{2}{3}$
- $\frac{3}{4} \times 20 = 15$
- $\frac{3}{4} \times \frac{20}{1} = \frac{15}{1} = 15$
- $5 \times \frac{3}{10} = 1\frac{1}{2}$
- $\frac{1}{8} \times \frac{3}{2} = \frac{3}{16}$
- $\frac{7}{8} \times 24 = 21$
- $\frac{7}{8} \times \frac{24}{1} = \frac{21}{1} = 21$

2. Find the product and write your answer as a mixed number.

- $6 \times \frac{4}{5} = 4\frac{4}{5}$
- $\frac{6}{1} \times \frac{4}{5} = \frac{24}{5} = 4\frac{4}{5}$
- $\frac{3}{5} \times 7 = 4\frac{1}{5}$
- $\frac{3}{5} \times \frac{7}{1} = \frac{21}{5} = 4\frac{1}{5}$

3. There are 30 apples in a basket. The farmer tells you  $\frac{5}{6}$  of them are Red Delicious. How many of the apples are Red Delicious?

$$\frac{5}{6} \times 30 = \frac{5}{1} \times 5 = 25$$

25 are Red Delicious

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## LESSON 26

The key skill in this lesson is being able to convert between improper fractions and mixed numbers. That will come up again in Lesson 27.

### Page 111 Answers

MULTIPLY MIXED NUMBERS LESSON 26

**LESSON 26: MULTIPLY MIXED NUMBERS**

Mixed Number Roll

**You Will Need:**

- Three dice

**You Will Do:** Sample Answers

- Roll the dice. The three numbers are going to be the whole number, the numerator, and the denominator of your mixed number below. You can write the results from the dice whenever you like, just make sure the numerator of the fraction is less than the denominator.
 

$3 \frac{2}{5} = \frac{17}{5}$
- Rewrite the mixed number as an improper fraction.
 

$4 \frac{5}{6} = \frac{29}{6}$

$5 \frac{1}{5} = \frac{26}{5}$

$3 \frac{5}{6} = \frac{23}{6}$
- Roll 3 more mixed numbers and then convert them to improper fractions. If you get a number for the denominator that you already did in a previous problem, roll again. You want to practice with 4 different denominators.

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### Page 113 Answers

MULTIPLY MIXED NUMBERS LESSON 26

Find each product. Write your answer as a mixed number.

$a. \frac{1}{3} \times 1\frac{3}{2} = \frac{1}{2}$ $\frac{1}{3} \times \frac{3}{2} = \frac{1}{2}$	$b. 1\frac{1}{3} \times 1\frac{1}{2} = 2$ $\frac{4}{3} \times \frac{3}{2} = \frac{2}{1} = 2$
$c. 1\frac{1}{3} \times 2\frac{1}{2} = 3$ $\frac{4}{3} \times \frac{5}{2} = \frac{20}{6} = \frac{10}{3} = 3$	$d. 1\frac{2}{3} \times 1\frac{1}{2} = 2$ $\frac{5}{3} \times \frac{3}{2} = \frac{5}{2} = 2$
$e. 1\frac{1}{5} \times \frac{3}{4} = \frac{9}{10}$ $\frac{6}{5} \times \frac{3}{4} = \frac{9}{10}$	$f. 1\frac{1}{6} \times 1\frac{1}{7} = 1\frac{1}{3}$ $\frac{7}{6} \times \frac{8}{7} = \frac{4}{3} = 1\frac{1}{3}$
$g. 1\frac{2}{4} \times 2\frac{1}{3} = 4\frac{1}{12}$ $\frac{7}{4} \times \frac{7}{3} = \frac{49}{12} = 4\frac{1}{12}$	$h. 2\frac{1}{3} \times \frac{3}{4} = 1\frac{3}{4}$ $\frac{7}{3} \times \frac{3}{4} = \frac{7}{4} = 1\frac{3}{4}$

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## LESSON 27

I love the visual of the opening activity. I don't think I ever really understood what dividing by a fraction meant until I was out of school. Fraction tiles make it so much easier to picture what is happening and why flipping the fraction and multiplying gives you the correct answer.

### Page 114 Answers

LESSON 27 DIVIDE FRACTIONS

**LESSON 27: DIVIDE FRACTIONS**

Dividing Fraction Tiles

**You Will Need:**

- Fraction tiles
- A blank sheet of paper
- Green, yellow, and blue markers (to be used later)

**You Will Do:**

- We are going to model the fraction division problem below. Start by tracing the 1 whole tile twice on the blank sheet of paper. This now represents 2.
 

$2 = 1\text{ tile} = 12$
- Trace the  $\frac{1}{5}$  tile to split the 1 whole into 5/6 sections. You are dividing the 2 whole tiles by  $\frac{1}{5}$ . How many sections were created? Write this number as the answer to the fraction problem below.
 

$2 \div \frac{1}{5} = 10$
- Trace 1 whole tile three times. Now divide it into 1/5 sections to act out the problem below. Write in the quotient.
 

$3 \div \frac{1}{5} = 15$

In the opening activity, you acted out what happens when we divide a whole number by a fraction. Mathematicians developed a simple process for dividing fractions without drawing a picture. When we divide fractions, we multiply by the reciprocal. Recall that the reciprocal of a fraction is the fraction flipped upside down. For example, the reciprocal of  $\frac{2}{3}$  is  $\frac{3}{2}$ . When you multiply reciprocals, the result is 1.

To divide by a fraction, multiply by the reciprocal.

**RECIPROCAL OF A FRACTION:** The upside-down version of a fraction is its reciprocal. When a number is multiplied by its reciprocal, the result is one.

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Page 116 Answers

**LESSON 27** DIVIDE FRACTIONS

**EXAMPLE 3:** Find the quotient,  $\frac{3}{4} \div \frac{5}{8}$

First, we will rewrite the problem as a multiplication problem with the reciprocal of the second fraction.

$$\frac{3}{4} \times \frac{8}{5} =$$

We can eliminate the common factor of 4 before we multiply.

$$\frac{3}{1} \times \frac{2}{5} =$$

Now we can multiply.

$$\frac{3}{1} \times \frac{2}{5} = \frac{3 \times 2}{1 \times 5} = \frac{6}{5}$$

Finally, we need to write our answer as a mixed number.

$$\frac{6}{5} = \frac{5}{5} + \frac{1}{5} = 1\frac{1}{5}$$

**1.** Write the reciprocal for each whole number or fraction.

a. 5 reciprocal =  $\frac{1}{5}$

b.  $\frac{7}{8}$  reciprocal =  $\frac{8}{7}$

c. 6 reciprocal =  $\frac{1}{6}$

d.  $\frac{7}{20}$  reciprocal =  $\frac{20}{7}$

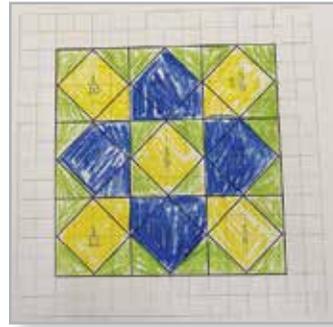
e. 4 reciprocal =  $\frac{1}{4}$

f.  $\frac{1}{19}$  reciprocal =  $19$

g.  $\frac{4}{5}$  reciprocal =  $\frac{5}{4}$

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Page 117 Answers



**LESSON 28**

This lesson is very similar to Lesson 15. The only difference is that the quotients are mixed numbers.

Page 118 Answers

**LESSON 28** DIVIDE WHOLE NUMBERS WITH FRACTION ANSWERS

**ACTIVITY**

**LESSON 28: DIVIDE WHOLE NUMBERS WITH FRACTION ANSWERS**

**Dividing Fraction Tiles**

**You Will Need:**

- Graham crackers

**You Will Do:**

1. We are going to model the division problem below with graham crackers. Begin by taking out 6 whole graham crackers. We want to divide them evenly between 4 people. Can you split the graham crackers so that each person receives the same amount? Draw a picture of what each person will receive below. Then write in the answer to the problem using fractions.

$6 \div 4 = \frac{3}{2}$  or  $1\frac{1}{2}$

2. Now let's model another division problem. Suppose you had 9 whole graham crackers and you wanted to divide them between 2 people. Can you split the graham crackers so that each person receives the same amount? Draw a picture of what each person will receive below. Then write in the answer to the problem using fractions.

$9 \div 2 = \frac{9}{2}$  or  $4\frac{1}{2}$

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Page 120 Answers

**LESSON 28** DIVIDE WHOLE NUMBERS WITH FRACTION ANSWERS

**ACTIVITY**

Find each quotient. Write your answer as a mixed number.

a.  $\frac{4}{29} \div \frac{1}{8} = \frac{32}{29}$

b.  $\frac{1}{58} \div \frac{5}{3} = \frac{3}{290}$

c.  $\frac{6}{425} \div \frac{24}{1} = \frac{1}{708\frac{1}{5}}$

d.  $\frac{11}{782} \div \frac{7}{12} = \frac{6}{708\frac{1}{5}}$

e.  $\frac{6}{533} \div \frac{30}{3} = \frac{2}{2665}$

f.  $\frac{4721}{20} \div \frac{1}{1} = \frac{4721}{20}$

g.  $\frac{13}{341} \div \frac{3}{11} = \frac{13}{1023}$

h.  $\frac{12}{786} \div \frac{7}{16} = \frac{16}{1023}$

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## LESSON 29

Again, in this lesson students have to be able to switch between mixed numbers and improper fractions and back again. Converting between different forms of a number is a key skill in mathematics.

Page 121 Answers

DIVIDE MIXED NUMBERS LESSON 29

**LESSON 29: DIVIDE MIXED NUMBERS**

**Splitting a Recipe**

**You Will Need:**

- A recipe

**You Will Do:**

- Clara is making perpendicular bread. She wants to cut the recipe in half. Use the pictures to help find how much of each of the ingredients she will need.

Original Recipe	Half as Much
1 $\frac{1}{4}$ cups water	_____ cups of water
$\frac{1}{2}$ cup molasses	_____ cup molasses
1 $\frac{1}{2}$ cups bread flour	_____ cup bread flour
2 $\frac{1}{2}$ teaspoons yeast	_____ teaspoons yeast

2. Use your recipe. Try dividing the amounts in half. Check your answer with your partner.

Original Recipe	Half as Much

Answers will vary.

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Page 124 Answers

LESSON 29 DIVIDE MIXED NUMBERS

**1. Rewrite each mixed number as an improper fraction.**

a.  $3 \frac{1}{3} = \frac{10}{3}$       b.  $2 \frac{1}{7} = \frac{15}{7}$

c.  $4 \frac{1}{2} = \frac{9}{2}$       d.  $1 \frac{7}{8} = \frac{15}{8}$

e.  $5 \frac{1}{3} = \frac{16}{3}$       f.  $2 \frac{1}{5} = \frac{13}{5}$

**2. Find each quotient.**

a.  $2 \frac{2}{3} + 4 = \frac{14}{3}$       b.  $1 \frac{2}{3} + 5 = \frac{17}{3}$

$\frac{14}{3} \times \frac{1}{4} = \frac{7}{6}$       c.  $\frac{17}{3} \times \frac{1}{5} = \frac{17}{15}$

d.  $3 \frac{1}{4} + 2 = \frac{17}{4}$       e.  $1 \frac{4}{5} + 3 = \frac{19}{5}$

$\frac{17}{4} \times \frac{1}{2} = \frac{17}{8}$       f.  $\frac{19}{5} \times \frac{1}{5} = \frac{19}{25}$

g.  $4 \frac{1}{3} + 4 \frac{1}{3} = 8 \frac{2}{3}$       h.  $2 \frac{1}{2} + 3 \frac{1}{2} = 6$

$\frac{17}{3} \times 4 = \frac{68}{3} = 22 \frac{2}{3}$       i.  $\frac{6}{2} \times \frac{1}{2} = \frac{6}{4} = 1 \frac{1}{2}$

j.  $4 \frac{3}{8} + 7 \frac{1}{11} = 11 \frac{38}{88}$       k.  $1 \frac{7}{8} + 4 \frac{3}{8} = 6 \frac{10}{8} = 7 \frac{1}{2}$

$\frac{35}{8} \times \frac{11}{7} = \frac{385}{56} = 6 \frac{7}{8}$       l.  $\frac{15}{8} \times \frac{4}{3} = \frac{60}{24} = 2 \frac{1}{2}$

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## LESSON 30

This lesson is just a mix of review, so students have another opportunity to practice.

Page 125 Answers

MIXED FRACTION REVIEW LESSON 30

**LESSON 30: MIXED FRACTION REVIEW**

**Improper Domino War**

**You Will Need:**

- Dominoes
- 2 players
- Lesson 30 Score Cards

**You Will Do:**

- Carefully use one of the activity sheets from the back of the answer key and cut it in half. Each player gets one score card. For all the dominoes face down in a pile. At the same time, both players flip over a domino. They write the domino as an improper fraction on their scoring sheet with the larger number in the numerator.
- Both players write the improper fraction as a mixed number. Whoever has the greater mixed number wins that round. Players can choose a partner if they are unsure about which mixed number is greater.
- Play 5 rounds. Whoever wins the most rounds out of the five wins the game.

**Practice your fraction skills in this mixed review.**

**1. Find the sum or difference.**

a.  $\frac{6}{8} + \frac{1}{8} = \frac{7}{8}$       b.  $\frac{5}{30} - \frac{3}{30} = \frac{2}{30} = \frac{1}{15}$

c.  $1 \frac{1}{3} + \frac{5}{6} = \frac{4}{3} + \frac{5}{6} = \frac{8}{6} + \frac{5}{6} = \frac{13}{6}$       d.  $2 \frac{1}{4} - 1 \frac{1}{2} = \frac{5}{4} - \frac{3}{2} = \frac{5}{4} - \frac{6}{4} = -\frac{1}{4}$

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Page 126 Answers

LESSON 30 MIXED FRACTION REVIEW

**2. Find the product. Simplify your answer.**

a.  $\frac{3}{4} \times \frac{4}{3} = 1$       b.  $\frac{1}{7} \times \frac{4}{7} = \frac{4}{49}$

c.  $\frac{1}{6} \times \frac{3}{11} = \frac{1}{22}$       d.  $\frac{1}{5} \times 2 \frac{1}{2} = \frac{1}{5} \times \frac{5}{2} = \frac{5}{10} = \frac{1}{2}$

**3. Find the quotient.**

a.  $\frac{7}{10} \div \frac{4}{5} = \frac{7}{10} \times \frac{5}{4} = \frac{35}{40} = \frac{7}{8}$

b.  $\frac{7}{10} \div 2 = \frac{7}{10} \times \frac{1}{2} = \frac{7}{20}$

c.  $1 \frac{1}{2} \div \frac{3}{4} = 2 \frac{1}{2} \div \frac{3}{4} = \frac{5}{2} \times \frac{4}{3} = \frac{20}{3} = 6 \frac{2}{3}$

d.  $2 \frac{1}{8} \div \frac{4}{3} = 3 \frac{1}{8} \div \frac{4}{3} = \frac{25}{8} \times \frac{3}{4} = \frac{75}{32} = 2 \frac{11}{32}$

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## CHAPTER 3 REVIEW

The Chapter 3 review is a quick way for you to see if your child is mastering the material. If they seem to be struggling with any of the concepts, you might want to take a day to review before moving onto the unit project. An optional Chapter 3 test is provided in the back of this answer key. If you plan on using it, give it to your child after he or she has completed the chapter review.

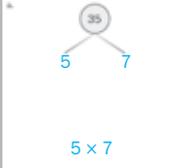
### Page 127 Answers

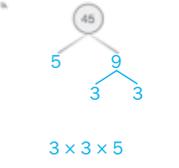
CHAPTER 3 REVIEW

**SKILLS CHECK**  
Circle all of the prime numbers in the list below.

1. 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 19  
20, 21, 22, 23, 24, 25

Write out the prime factorization of each number.

a.   $5 \times 7$

b.   $3 \times 3 \times 5$

1. Find the sum or difference.

a.  $\frac{1}{24} + \frac{1}{24} = \frac{2}{24} = \frac{1}{12}$   
 $\frac{16}{24} + \frac{9}{24} = \frac{25}{24}$

b.  $\frac{9}{10} - \frac{6}{10} = \frac{3}{10}$   
 $\frac{9}{10} - \frac{6}{10} = \frac{3}{10}$

c.  $1\frac{1}{4} + 1\frac{1}{3} = 2\frac{7}{12}$   
 $\frac{5}{4} + \frac{4}{3} = \frac{15}{12} + \frac{16}{12} = \frac{31}{12}$

d.  $2\frac{1}{8} - 1\frac{5}{8} = \frac{1}{8}$   
 $\frac{17}{8} - \frac{13}{8} = \frac{4}{8}$

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### Page 128 Answers

REVIEW CHAPTER 3

2. Find the product or quotient.

a.  $\frac{1}{3} \times \frac{6}{7} = \frac{2}{7}$   
 $\frac{2}{3} + \frac{1}{3} = \frac{3}{3} = 1$   
 $\frac{2}{3} \times \frac{3}{2} = \frac{6}{6} = 1$

b.  $\frac{5}{12} + 5 = \frac{5}{12} + \frac{60}{12} = \frac{65}{12}$   
 $\frac{5}{12} \times \frac{1}{5} = \frac{1}{12}$   
 $\frac{1}{4} \times \frac{4}{5} = \frac{4}{20} = \frac{1}{5}$   
 $\frac{7}{4} \times \frac{4}{5} = \frac{28}{20} = \frac{7}{5}$

3. Complete the chart.

Fraction	Decimal
$\frac{1}{2}$	0.5
$\frac{4}{10} = \frac{2}{5}$	0.4
$\frac{4}{5}$	0.8
$\frac{1}{3}$	0.333...
$\frac{3}{4}$	0.75

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## UNIT 1 PROJECT

Students can make any type of design that they like. This art connection is a fun change of pace after so much decimal and fraction work.

### Page 129 Answers

UNIT 1 PROJECT

**UNIT 1 PROJECT: GEOMETRIC ART**

**You Will Need:**

- Unit 1 Project Activity Sheet
- Markers
- Scissors
- Glue

**You Will Do:**

**Step One:** Carefully tear out the activity sheet from the back of the answer key. Color in the Hundreds Grid using whatever design you like. Just don't use more than 7 different colors and only use one color in each small square.

**Step Two:** Once your design is finished, list the colors you used in the left-hand column of the chart below. Then count how many squares you colored in that color.

Color	Number of Squares	Fraction	Decimal

Answers will vary.

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### Page 130 Answers

PROJECT UNIT 1

**Step Three:** What fraction of your chart is colored in each color? List that in the next column. Make sure you reduce the fraction.

**Step Four:** In the last column, write the same amount as a decimal. Have your parent check your answers.

**Step Five:** Share your design and your knowledge of fractions and decimals with family and friends. Then cut it out and glue it below.

Answers will vary.

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## COMPLETE SUPPLY LIST

- Fraction tiles
- A protractor
- Colored pencils
- Numbered cards 3-10
- Notecards
- Scissors
- Beans
- Four-operation calculator
- Dice
- Glue
- Game pieces
- A takeout menu
- An envelope
- Dominoes
- Graham crackers
- A recipe
- Markers
- Bingo chips
- A paper clip
- A miniature bag of Skittles®
- Fruit salad
- A bowl
- A quarter
- Four different kinds of beverages
- Similar items from two different grocery stores
- Thick string, yarn, or a thin piece of ribbon
- A bobbin
- A chenille stem
- A small plastic cup
- A pair of sharp scissors or a knife
- A stopwatch
- Measuring tape
- Pennies, marbles, or other small weights
- Several food items from your refrigerator or pantry
- A store flyer or magazine
- A tape measure
- Ice cubes
- Salt, sugar, baking soda
- 5 transparent cups
- 5 labels
- A tablespoon
- A permanent marker
- Colored pencils
- Glue stick
- A deck of cards
- A Monopoly™ gameboard
- An analog thermometer
- Masking tape
- Sticky notes
- 2 blank sheets of poster board
- World almanac or access to the internet for research
- A printer
- 3 sheets of 8.5 × 11" colored paper
- A stapler
- A sheet protector
- A ruler
- A highlighter
- A set of 3D shapes (including a sphere, a cone, a cylinder, and several types of pyramids and prisms)
- A box (it can be any size)
- Rectangle or square shapes (magnetic tiles, the green triangles from a pattern block set, or triangles that are the same size and shape cut out of cardboard)
- A refrigerator (or another larger, rectangular object to measure, like a deep freeze or a dresser)
- A bag of small marshmallows
- Several pieces of card stock or thick paper